# Whither Consequence?

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Abstract: There are brief passages in Fallacies which suggest that Hamblin may doubt the existence of the inductive consequence relation. If so, his view would be that when an inductive inference is correct, it is not made so by the fact that its conclusion is an inductive consequence of its premisses. It would follow accordingly that correct conclusiondrawing needn't be a matter of correct consequence-drawing. If in turn that were so, perhaps the same could be said for plausibility and defeasibility conclusion-drawing. This generates this paper's central question: Under what conditions does a consequence relation exist between the premisses and conclusion of a correct inference?

Résumé: Il y a de brefs passages dans Fallacies qui suggèrent que Hamblin doute de l'existence de la relation de conséquence inductive. Si oui, son point de vue serait que si une inférence inductive est correcte, ce n'est pas le fait que sa conclusion est une conséquence inductive de ses prémisses qui rend l'inférence correcte. Il s'ensuivrait que tirer une conclusion correctement n'est pas nécessairement une affaire de tirer une conséquence correctement. Si c'était le cas, peut-être la même chose pourrait se dire de tirer des conclusions plausibles ou annulables. Cela fait soulever une question centrale de cet article: Dans quelles conditions une relation de consé-quence existe entre les prémisses et la conclusion d'une inférence correcte?

**Keywords:** consequence, conditionality, defeasibility, deduction, entailment, induction, probability, plausibility

## 1. Hamblin's Question

As of this writing in late 2010, Charles Hamblin's *Fallacies* is forty years old. There is a large research programme and a hefty body of work that owes much to its influence. *Fallacies* is not a perfect book. But, these four decades later, it lacks an equal.

One of *Fallacies*'s more interesting assertions is that we in the present-day are in the same situation as our pre-12<sup>th</sup> century forbears. They had lost the logical theory of the Ancients, and

we have lost fallacy theory.<sup>1</sup> Actually, he says, this comparison is not quite right. In the case of the logic of deduction, there was something to *be* lost. But there has never been a theory of the fallacies. Even those from whom the most important pre-1970 contributions were to come were comparative dabblers.<sup>2</sup> Hamblin is dissatisfied with this state of affairs. It is a scandal that "[w]e have no theory of fallacy at all in the sense in which we have theories of correct reasoning or inference." (p. 11)<sup>3</sup> Hamblin calls upon logicians to erase this embarrassment.

This raises some obvious questions, three of which are especially interesting. One is why, in 1970, the fallacies had yet to attract a full-blown theory. A second is whether, provided it had the will for it, "our" logic—modern logic<sup>4</sup>—would possess the wherewithal to repair this omission. Assuming a negative answer, the third of Hamblin's questions would be whether a proper theory of the fallacies could be had beyond the borders of modern logic, indeed beyond the borders of *any* logic, "ours", "theirs" or "yet to come". For ease of reference, and when the context allows it, I shall speak of these collectively as *Hamblin's Question*.

The very fact that there was a Hamblin's Question to ask suggests that the fallacies posed for the would-be theorist a special kind of difficulty. Virtually everything a logician turns his hand to is difficult. This is partly a matter of the conceptual complexity of logic's target properties and also, even more, a consequence of its strict demands for precision, rigour and systematicity. Hardly anything that excites a human being's intellectual interest makes the "logical cut." No one seriously supposes, except in a lazily metaphorical way, that there is a logic of love, or of beauty or of justice. (There is, for example, nothing to be learned about what in actuality is right or wrong from deontic logic. At their best, deontic logics hold a certain technical interest. But on matters of moral substance they are non-starters.<sup>5</sup>)

<sup>&</sup>lt;sup>1</sup> Hamblin writes: "In some respects, ..., we are in the position of the medieval logicians before the twelfth century: we have lost the doctrine of fallacy, and need to recover it." (p. 11)

<sup>&</sup>lt;sup>2</sup> Hamblin writes: "Strangely, in a certain sense, there has never been a book on fallacies; never, that is, a book-length study of the subject as a whole, or of incorrect reasoning in its own right rather than as an afterthought or adjunct to something else." (p. 10)

<sup>&</sup>lt;sup>3</sup> To catch Hamblin's meaning here, it is advisible to read "correct" with a contrastive stress.

<sup>&</sup>lt;sup>4</sup> Let modern logic be any of the established systems in the period ensuing from the publication in 1879 of Frege's *Begriffsschrift* to the present.

<sup>&</sup>lt;sup>5</sup> The same, it seems to me, is also true of epistemic and doxastic logic. If you have an *epistemologist's* curiosity about knowledge and belief, these are the last places to satisfy it. See here my "Making too much of worlds", in Guido

Some things are clearly amenable to logical treatment the *consequence* relation, for example, or the *provability* property—and others, indeed most others, clearly are not. There are no algorithms for this. Logic-worthiness is not a decidable property. There are borderline cases which underdetermine the in-out question. (Think here of the concept of *plausibility*.)<sup>6</sup> There are also cases which we might characterize as "crossborder". These are concepts which appear to make as much of a claim on disciplines other than logic as on logic itself. (Think here of the concept of *inference*.)<sup>7</sup>

We have it, then, that one level of indecisiveness about the logic-worthiness of a concept is not knowing—or having principled reason to say—whether it's in or out or in-between and, if in-between, whether a borderline or cross-border case. But there is also a higher level of theoretical uncertainty, in which the aspiring theorist simply has *no idea* of how to proceed, never mind how his progress, if there were any, would best be classified afterwards. What I mean by this is the far from uncommon circumstance in which someone produces a not implausible account of something without having much of a clue, before or after, about how to answer the question: "What does it take to make a good theory of that?" or, more directly, how to respond to the instruction: "State and justify your methodology, please."

It is interesting that much of *Fallacies* reads as if the logician's problem with fallacy theory is not indecisiveness at *either* of these levels, but rather the comparative security of thinking that fallacies are excluded by the fact that "we [logicians have] set ourselves higher standards of theoretical rigour and will not be satisfied for long with a theory less ramified and systematic than we are used to in other departments of Logic …" (p. 12). What this suggests is that the fallacies, like most other things, aren't logic-worthy. They won't yield to the strict demands that a logic imposes on its subject matter. Consider now the words that immediately follow:

<sup>7</sup> If Harry infers  $\psi$  from a set of sentences  $\Sigma$ , it is a matter of logic as to whether  $\psi$  actually follows from  $\Sigma$ . But might it also be a matter of epistemology as to whether drawing that consequence is a reasonable thing to do, or a matter of psychology as to whether drawing it lies within Harry's computational powers? For more on the difference between consequence-having and consequence-drawing see section 4.

Imaguire and Dale Jacquette, editors, *Possible Worlds*, pages 171-217, Munich: Philosophia, 2010.

<sup>&</sup>lt;sup>6</sup> Plausibility sometimes is taken as an operator-operator, as in "plausibly follows from", and sometimes as a sentence-operator, as in "Vulcan was a plausible hypothesis in La Verrier's day". Perhaps it is both. Whether it is or not, some would exclude it from logic on the ground that there is no negation function definable for plausibility. For are there not equally plausible but incompatible propositions? I will return to plausibility in section 8 below.

... one of the things we may find is that the kind of theory we need cannot be constructed in isolation from them [= the departments of logic]. (p. 12)

This, if true, would be bankrupting news for fallacy theory. For if the concept of fallacy is not a concept for logic in any of its departments and yet "in isolation" from logic a theory of the fallacies can't be produced at all, then it would appear that the fallacies don't admit of theoretical treatment of any kind; that the very idea of a theory of them is dead-on-arrival.

By any standard of fair comment, this is pretty sloppy going. Why, if it were his position that a theory of fallacies cannot be got at all, would Hamblin have favoured us with a whole book on them? If Fallacies contained no theory of its subject matter, what would have been the value of it? Virtually everyone agrees that *Fallacies* is a good book, and that there is much to learn from it. This gives us two possibilities to consider. One is that *Fallacies is* a theory of the fallacies, indeed a theory that preserves the traditional idea that to commit one is to make a mistake of logic. The other is that *Fallacies*, though informative, sensitive to distinctions, mindful of historical developments and thoughtfully reasoned, is not a *theory*. Whichever it might be, each is a discouragement of the very presupposition of Hamblin's Question. If the first possibility held true, the mere asking of it would be the fallacy of complex question. Yet if the other possibility obtained, Hamblin's Question would lack a motivation, and we would be left to scramble for a face-saving way out-for example, by interpreting the Question as asking why fallacy theory can't be formal in the manner of, say, classical first order logic or the ZF theory of sets. This is not very satisfying. Hasn't it been recognized since the very beginnings of systematic logic that most of the fallacies (and all of the interesting ones) are informal, made so by considerations other than, or over and above, their logical forms—if such there be?

There is point in reminding ourselves that *Fallacies* is in the first instance a complaint by a logician about logic. The complaint is that logic has abandoned the fallacies research programme. In the second instance, *Fallacies* is puzzled recognition that logicians never actually got around to it in the first place, not at least in a theoretically robust way.<sup>8</sup> There is a good deal

<sup>&</sup>lt;sup>8</sup> Hamblin died in 1985 at a regrettably early age. This denied to the fallacies community the benefit of his commentary on treatments which were inspired in no small way by his demand for renewal but which appeared after his death. See, for example, John Woods and Douglas Walton, *Fallacies: Selected Papers 1972-1982*, 2<sup>nd</sup> edition, with a Foreword by Dale Jacquette, London: College Publications, 1989/2008, Douglas Walton, *A Pragmatic* 

of difference between the complaint and the bewilderment. But even so, it does appear that Hamblin's position is that:

*Hamblin's view*: If a theory of fallacies is possible at all, it is the job of logicians to produce it. As it happens, it is not in fact unreasonable to suppose that a theory of the fallacies is indeed possible. So activating the fallacies project is a reasonable demand on logic.

It becomes a question of rather central importance whether *Fallacies* itself counts as a response to this imperative.

## 2. The departments of logic

Fallacies appeared in 1970, in the midst of the greatest theoretical proliferation in logic's long history. Hamblin himself acknowledges that logic has "departments". He would have been fully conversant with developments in intuitionist, many valued, modal, epistemic and temporal logic, and could not have been unaware of the turbulence, caused in large part by his compatriots, of relevant and paraconsistent logics. Dialethic logic, another antipodean disturbance, didn't hit the mainstream until 1979, with the appearance in the Journal of Philosophical Logic of Graham Priest's "The logic of paradox",9 but there were earlier intimations of it abundantly available and widely discussed. not least in places like Australia. By 1970, there weren't many logicians who hadn't encountered this explosion in logic, even if not enthusiastic abettors of it.<sup>10</sup> Logic was now a store with many departments-a veritable Selfridges or Macy's-giving the would-be logical theorist the gift of easy credit and non-stop shopping.

In the aftermath of *Fallacies* from 1972 to 1985, Douglas Walton and I published some twenty five papers in which we took Hamblin's call as permitting, if not strictly demanding, the appropriation of this abundance to the shifting analytical re-

<sup>9</sup> Volume 8, pages 219-241.

*Theory of Fallacy.* Tuscaloosa: University of Alabama Press, 1995, Frans van Eemeren and Rob Grootendorst, *Argumentation, Communication, and Fallacies: A Pragma-Dialectical Perspective.* Mahwah, NJ: Erlbaum, 1992, and John Woods, *The Death of Argument: Fallacies in Agent-Based Reasoning,* Dordrecht and Boston: Kluwer, 2004.

<sup>&</sup>lt;sup>10</sup> Quine is perhaps the most notable exception. But even he grudgingly allows for the possibility that intuitionism is a real logic, and the virtual certainty that quantum logic must now be acquiesced to. See W.V. Quine, *Philosophy of Logic*, 2<sup>nd</sup> edition, Cambridge, MA: Harvard University Press, 1986; first published in 1970, and *Pursuit of Truth*, 2<sup>nd</sup> revised edition, Cambridge, MA: Harvard University Press, 1992. First published in 1990.

quirements of fallacious reasoning. In what would come to be known as the Woods-Walton Approach, the main organizing idea was that at least one of the reasons why logic hadn't beforehand made satisfactory headway with the fallacies was that it had lacked the well-stocked inventories of concepts and techniques which flowed from its new pluralism. One of the systems the WW-Approach made brisk use of was intuitionist logic, with some borrowings from Kripke's modal semantics. Intuitionist logic had been around—and influential—since the first decade of the century just past, and Kripke semantics had burst onto the scene beginning in 1959.<sup>11</sup> So in 1970 these logics were hardly all that new.

Also dating from 1959 was the Yale-Pittsburgh-Canberra upsurge in relevant and paraconsistent logic,<sup>12</sup> which with only slight exceptions<sup>13</sup> made no major inroads to the WW-Approach—an embarrassing omission, given the widespread insistence that a number of the more important fallacies are errors of relevance and that premisses need be (or need not be!) both consistent and relevant. Negation-as-failure cropped up in our 1978 paper on the *ad ignorantiam*, but it was our invention, not a borrowing from autoepistemic logic, which didn't exist yet.<sup>14</sup> Another of WW's more frequent appropriations, and the

<sup>&</sup>lt;sup>11</sup> Saul Kripke, "A completeness theorem in modal logic", *Journal of Sumbolic Logic*, 24 (1959), 1-15; "Semantical analysis of modal logic, I: Normal propositional calculi", *Zeitschrift für Mathematische Logik und Grundlagen der Mathematik*, 8 (1963), 113-116; "Semantical considerations in modern modal logic", *Acta Philosophica Fennica*, 16 (1963), 83-94; "Semantical analysis of modal logic, II: Non-normal modal propositional calculi." In J.W. Addison, L. Henkin and A. Tarski, editors, *The Theory of Models*, pages 202-220. Amsterdam: North-Holland, 1965; and "Semantical analysis of intionistic logic". In J. Crossley and M. Dummett, editors, *Formal Systems and Recursive Functions*, pages 92-130. Amsterdam: North-Holland, 1965.

<sup>&</sup>lt;sup>12</sup> A.R. Anderson and Nuel D. Belnap, Jr., "A simple treatment of truth functions", *Journal of Symbolic Logic*", 24 (1959), 301-312; A.R. Anderson, "Completeness theorems for the systems *E* of entailment and *EQ* of entailment with quantification", *Zeitschrift für Mathematische Logik und Grundlagen der Mathematik*, 6 (1959), 201-216; Nuel D. Belnap, Jr., "*EQ* and the first order functional calculus", same journal, 6 (1960), 217-218; and "Intentional models for first-degree formulas", *Journal of Symbolic Logic*, 32 (1967), 1-22. See also Richard Epstein, "Relatedness and implication", *Philosophical Studies*, 36 (1979) 137-173.

<sup>&</sup>lt;sup>13</sup> "On fallacies", which appeared in 1972; it is chapter 1 of *Fallacies: Selected Papers* (1989/2007). See also "Why is the *ad populum* a fallacy?" (1980, chapter 16 of *Fallacies: Selected Papers*); "Post hoc, ergo propter hoc" (1977), chapter 9; and "Question-begging and cumulativeness in dialectical games" (1982, chapter 19).

<sup>&</sup>lt;sup>14</sup> "The fallacy of *ad ignorantiam*" is chapter 11 of *Fallacies: Selected Papers*. Autoepistemic logic arises from contributions by R.C. Moore in 1984 and 1988—"Possible worlds semantics for autoepistemic logic", *Proceedings of the Non-monotonic Workshop*, New Palz: NY, 1984. 344-354, and "Autoepistemic logic", in P. Smets, E.H. Mamdani, D. Dubois and H. Prade, edi-

one most directly inspired by Hamblin himself, was dialogue logic (or in a variation, dialectic).<sup>15</sup> Later on I will have something to say about dialogue logic. The point to stress here is that according to the WW-Approach, dialogue logics are but one of the frameworks available for the analysis of concepts of rightful interest to logicians.

The WW-idea that there is no single logical system, or type of logic, sufficient to account for all the fallacies, and that only a pluralism in logic will enable the trick to be turned, hasn't won much support in the years following its flotation. One of the criticisms leveled against it is that it fails to provide a unitary theoretical framework for the fallacies, in effect necessitating the working up of a new logic for each different fallacy.<sup>16</sup> A further development has been Douglas Walton's slimmed-down relativization of the more sprawling pluralism of the WW-Approach to variations expressible within a generalized dialogical framework.<sup>17</sup> Seen the old way, dialogue logic is the right tool—organon—for some of the fallacies. Seen in Walton's newer way, dialogue logic is the right overall framework for them all.

Yet another important factor has been the indecisiveness of informal logicians about the extent to which the analysis of the fallacies is strictly a matter for dialogue logic, and also about where to draw the boundaries between informal logic and other disciplines that might be expected to bear on the fallacious.<sup>18</sup> A further complication is the ambivalence shown by the informal logic community about the place of formal methods in the analysis of the fallacies, or about the priorities that respectively at-

editors, Non-Standard Logics for Automated Reasoning, London: Academic Press, 1988.

<sup>&</sup>lt;sup>15</sup> Here I follow the contemporary convention by which dialectical exchanges are dialogues centred upon the disposition of disagreement.

<sup>&</sup>lt;sup>16</sup> This is a recurrent criticism advanced by the Pragma-Dialectical School against the WW-analysis. For a typical expression of it, see Frans van Eemeren and Rob Grootendorst's *Argumentation, Communication, and Fallacies,* p. 103. This is not the place to answer the objection in any detail. But perhaps it might quickly be observed that the principal appeal of the pluralist thesis is precisely the conviction that there *is* no unified logic of the fallacies. So the form of this dispute is, shall we say, negatively instructive. WW: "Since there is no unitary treatment for the fallacies, pluralism is the way to go." VEG: "Since it can't produce a unified treatment of the fallacies, pluralism isn't the way to go." ("VEG" compacts "van Eemeren" and "Grootendorst".)

<sup>&</sup>lt;sup>17</sup> See again his A Pragmatic Theory of Fallacy.

<sup>&</sup>lt;sup>18</sup> A leading example is posed by the question of where informal logic leaves off and pragma-dialectics comes into play. See also Ralph Johnson's *The Rise of Informal Logic*, Newport News, VA: Vale Press, 1996.

attach to the formal and informal aspects of their analyses.<sup>19</sup> All the same, I hardly need say that, like *Fallacies* itself, some of the very best work on the fallacies comes from this community.<sup>20</sup>

## **3. Induction: A puzzle**

Part of the modern subject's proliferation is to be found in a more or less standard family of inductive logics. Here, too, it would only seem natural that logician would look to these precincts for suitable accommodation of the inductive fallacies. However, it surprises me that, on a fair reading, Hamblin's logical sophistication appears to have deserted him in the matter of induction. He writes:

The difficulty that surrounds the definition of 'inductive fallacies' in their [sic] own right is that of distinguishing at all precisely between good inductions and bad. (p. 47)

In chapter 7, Hamblin takes up a related point:

Is there such a thing as inductive validity, or is it a contradiction in terms? Although we [= Hamblin] accept in principle that some inductive arguments are better than others, what are the canons by which we judge an inductive argument's absolute, rather than relative, worth? (p. 225)

A page later he adds:

A prior question ... in the case of inductive arguments is: *Are they real arguments*? (Emphasis in the original)

Hamblin identifies his difficulty with Hume's Problem, and he rebukes the Port Royal logicians for failing to find criteria (or canons) for its mitigation. This is problematic. Hume's Problem

<sup>&</sup>lt;sup>19</sup> Concerning which see, first, my "What is informal logic?", published in 1980, reprinted as chapter 17 of *Fallacies: Selected Papers;* and, second, "The informal core of formal logic", which is chapter 3 of *The Death of Argument: Fallacies in Agent-Based Reasoning.* 

<sup>&</sup>lt;sup>20</sup> See, for example, Ralph Johnson, *Manifest Rationality: A Pragmatic Theory of Argument*, Mahwah, NJ: Lawrence Erlbaum, 2000; James Freeman, *Acceptable Premises: An Epistemic Approach to an Informal Logic Problem*, Cambridge: Cambridge University Press, 2005 and Maurice Finocchiaro, *Arguments About Arguments: Systematic, Critical and Historical Essays in Logical Theory*, Cambridge: Cambridge University Press, 2005. Straddling the divide between the formal and informal is *Commitment in Dialogue*, by Walton and Erik Krabbe, published in 1995 by the SUNY Press.

is only tangentially about criteria. It is more centrally a problem about justification. Hume is sceptical about the defence of a quite general practice in which criteria for good and bad inductions are routinely and confidently applied. Hume's Problem is not about whether this, that or the other *is* a criterion of good inductive reasoning. The question is whether the goodness of a criterion can be *proved*. Hamblin's brief remark suggests that he himself thinks, approvingly, that Hume's point is that a criterion can't be good unless this strict test is passed. This seems to me excessive on both their parts. Nor can it be true that the Port Royal logicians were over-casual about finding criteria, as the sections on probability in *La Logique* make plain.<sup>21</sup>

In 1970, as now, no one would say that inductive logic is as securely tethered and well-advanced as the established families of deductive logic. But Carnap's ground-breaking Logical Foundations of Probability appeared in 1950, was followed two years later by A Continuum of Inductive Methods, after some papers of importance in 1945.<sup>22</sup> All this was preceded by J.M. Keynes' A Theory of Probability in 1921, not to overlook the masterly A System of Logic<sup>23</sup> by Mill in 1843, a work for which Hamblin has scant affection. All these works forward what they take to be binding criteria for inductive reasoning, yet none represents itself as the definitive solution of Hume's Problem. What, then, are we to make of Hamblin? It is not credible that he would have been unaware of the criteria advanced by the inductive logics of his day. I suppose, then, his is the stronger objection that the going inductive criteria are of no avail in the absence of a clinching and non-circular solution of the Problem of Induction. This is unsatisfying. Hamblin appears to be unacquainted with a companion "problem" for deduction, which demands a clinching and non-circular (hence non-deductive) demonstration that our going deductive criteria are actually sound. I hope that I have misunderstood Hamblin on this point.

Just lines after the quoted remarks the argument shifts. He writes:

Until it is clear whether induction is an argument-form in *any* way comparable with deduction there is nothing to be gained by

<sup>&</sup>lt;sup>21</sup> Almost certainly written by Pascal.

<sup>&</sup>lt;sup>22</sup> The two books are from the University of Chicago Press in 1950 and 1952 respectively. *Logical Foundations* had a second edition with the same publisher in 1962. Carnap's earlier papers include "On inductive logic", *Philosophy of Science*, 12 (1945), 72-97, and "The two concepts of probability", *Philosophy and Phenomenological Research*, 5 (1945), 513-532.

<sup>&</sup>lt;sup>23</sup> Published respectively by Macmillan in London and Longmans Green, also of London.

treating inductive shortcomings as varieties of fallacy (47). (Emphasis added.)

On the face of it, the incomparability worry is baffling. No one doubts that there are respects in which induction fails comparison with deduction. It fails comparison in the way that apples fail comparison with oranges. Differences there surely are between deductive reasoning and inductive reasoning. But does any of these actually disqualify inductive errors from membership in the class of fallacies? Hamblin gives us no help here. Perhaps he thinks the point is clear and persuasive just as it stands.

It is neither, made so in part by Hamblin's failure to specify the point of incomparability that disturbs him so, and the concomitant failure to distinguish between the claim that

1. the trouble that the incomparability poses for the fallacies is that there aren't (or probably aren't) any inductive ones

and the claim that

2. the trouble caused by the incomparability is not that there aren't any inductive fallacies but rather that there isn't (or probably isn't) a *logic* of them

and the further claim that

3. the trouble caused by the incomparability is that there isn't (or probably isn't) any logic of *induction*.

I am inclined to discount (1), that is to say, to discount it on Hamblin's behalf.<sup>24</sup> (2) and (3) are more interesting. What might we make of (2)? If it were true, then the following would also be true:

*The fallacy-excluding difference*: There is at least one feature D that deduction has and induction lacks which precludes there being a logic of the inductive *fallacies* and does not preclude there being a logic of the deductive fallacies.

It is the same were (3) to be true:

<sup>&</sup>lt;sup>24</sup> It would be different if Hamblin were the Aristotle of *Topics* and *the Sophistical Refutations*. The fallacies there are defined as errors of deduction. They are nearly always the mistaking of a non-syllogism for a syllogism, and sometimes are the error of misidentifying a proposition's contradictory.

*The logic-excluding difference*: There is at least one feature D that deduction has and induction lacks which precludes there being a *logic of induction* and does not preclude there being a logic of deduction.

Of course, it hinges on D. But it also hinges on a question which precedes Hamblin's Question. It is, as we might say,

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The Bigger Question: What does it take to make for a log-ic?
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This is the question I'll take up in the section to follow. Tracking down D is the business of the section after it.

#### 4. Logic's C-concepts

There was a time when the Bigger Question would have seemed a stupid question. Not now. The gluttony of logic's pluralism in the present day makes this a central issue for theory.<sup>25</sup> It is a question on the minds of some informal logicians, but not I think to much avail overall. Not dealing with it at all, it is even less availing for Hamblin.

Since its inception, the central focus of logic has been on the relations—one or more—of logical *consequence* or following from. In a coinage of Moore, the converse of consequence is entailment.<sup>26</sup> Usage varies here. In the deductive realm alone, logicians invoke the names of logical consequence, formal consequence, deductive consequence, semantic consequence, strict consequence, relevant consequence, paraconsistent consequence, and so on. Beyond deduction, a further miscellany awaits: inductive consequence, probabilistic consequence, abductive consequence<sup>27</sup>, nonmonotonic consequence, defeasible consequence, plausibilistic consequence, and what have you.

<sup>&</sup>lt;sup>25</sup> For some recent discussions of logical pluralism, see J.C. Beall and Greg Restall, *Logical Pluralism*, New York: Oxford, 2006, Hartry Field, "Pluralism in logic", *Review of Symbolic Logic*, 2 (2009) 342-359 and my "Mac-Coll's elusive pluralism", in Amirouch Moktefi and Stephen Read, editors, *Hugh MacColl After One Hundred Years, pages 205-233;* a special issue of *Philosophia Scientiae*, 15 (2011).

<sup>&</sup>lt;sup>26</sup> G.E. Moore, *Philosophical Studies*, London: Routledge and Kegan Paul, 1922.

<sup>&</sup>lt;sup>27</sup> In this paper I'm going to give abductive consequence a pass. Interested readers could consult my "Recent developments in abductive logic", *Studies in History and Philosophy of Science*, available online, January, 2011, and "Cognitive economics and the logic of abduction", *Review of Symbolic Logic*, in pess.

Over its long sweep, it would not be too much to say that consequence is the concept that anchors logic. It anchors it in the following way:

*K-consequence.* Let r denote reasoning of kind k—deductive, inductive, plausibilistic, defeasible, and whatever not. Then if r is logic-worthy, there will exist a relation of k-consequence peculiar to the type of reasoning that r is.

Pluralism sanctions a two-faced multiplicity about consequence. It allows for it to vary in general type—between, as we have seen, deductive and inductive consequence, and so on. The other face of pluralism shows itself *within* these types. They are intratype variations of those genera. Think here of the different provisions made for deductive consequence by classical, modal, many valued, intuitionist, free, relevant, paraconsistent and dialethic approaches, and of the still further variations within each of these—not only different but often enough incompatible. The same tale repeats itself for the other genera of consequence—inductive, abductive, defeasible, and the rest.

All this makes for a veritable blizzard of purported consequence relations. Even so, there is a distinction that runs through these different kinds and variations, comparatively untroubled by the resultant pluralism. This is the distinction between

1. consequence-having

and

## 2. consequence-drawing.<sup>28</sup>

Concerning (1) it suffices to say that whenever a statement  $\psi$  is a consequence of a (set of) statement(s)  $\Sigma$ , it is always true to say that  $\psi$  is a consequence that  $\Sigma$  *has*. Describing the drawing

<sup>&</sup>lt;sup>28</sup> The first logician to draw and attach importance to the distinction between consequence-having and consequence-drawing was Aristotle, though not in these words. In the earliest writings on the syllogism, Aristotle distinguishes between arguments whose premisses necessitate their conclusions (i.e., whose conclusion are consequences of those premisses) and arguments whose premisses not only necessitate their conclusions, but also satisfy further conditions. One is that none of the premisses be redundant. Another is that no premiss may occur as conclusion. A third forbids multiple conclusions. When these (and some other) conditions are met, the argument in question is a syllogism (*Topics*, 1, 100<sup>a</sup> 25-27 and *On Sophistical Refutations*, 1, 165<sup>a</sup> 1-3; see also *Prior Analytics*, A24<sup>b</sup> 19-22). Syllogisms have a number of interesting properties. One is that while a set of premisses may have many deductive consequences, it can syllogistically imply very few of them at most.

of consequences takes more care. There are two basic camps about consequence-drawing. According to the All-camp, it is rationally required, or at least permitted, to draw all the consequence had by anything  $\Sigma$  you currently believe or are otherwise committed to.<sup>29</sup> According to the Some-camp, it is never rationally required, or permitted, to draw all of  $\Sigma$ 's consequences, and yet, depending on the circumstances, it is sometimes rationally required, or permitted, to draw some of them.

Counting against the All-camp is the evident impossibility of any human individual actually doing its bidding. Against this, in turn, is the All-camp's propensity to impose its requirements not on living-and-breathing real-word reasoners, but rather on idealized reasoners, and to chalk up the shortfalls of the actual in relation to the ideal to the rational discredit of those who fall short. This dim view of the actual reasoner flows from the assumption, widely held within the All-camp, that the ideal standards sanctioned by the model, though not satisfied by actual reasoners, are *normatively binding* on them. The trouble with this is the near-wholesale indifference of ideal-modellers to the necessity of showing this assumption to be true. If, for example, a model provides that ideal reasoners close their beliefs under consequence, it cannot imaginably be inferred from this that the actual reasoner's inability to follow suit makes for a normatively subpar performance, if not out-and-out irrationality. That is, it cannot be inferred in the absence of a demonstration.<sup>30</sup> When a logician asserts that reasoning on the ground is defective when it proceeds in the absence of perfect information or it ignores propositions that are in the deductive closure of what he already believes, someone is guilty of defective reasoning. Either the reasoner on the ground is or the logician who makes the accusation is. Why should we automatically defer to the latter? Why should that be our default position? Isn't something more required? Don't we have need of a demonstration?

Consequence-drawing depends on consequence-having. I cannot draw  $\psi$  as a consequence of  $\sum$  if  $\psi$  isn't one of the consequences  $\sum$  actually has. If the Some-camp is right, the dependency doesn't run in the other direction.  $\sum$  has lots of consequences that no one will ever draw, or should or could. Given the *k*-consequence principle, we can now put it that

<sup>&</sup>lt;sup>29</sup> Subject, of course, to particular structural limitations. Not even the most ideal of ideal reasoners could draw as consequences all the truths of formal first-order arithmetic.

<sup>&</sup>lt;sup>30</sup> For some failed attempts to provide such demonstrations see my paper with Gabbay, "Normative models of rationality: The disutility of some approaches", *Logic Journal of the IGPL*, 11 (2003), 597-613.

*The consequence specification requirement*: The first task of a logic is to specify the consequence relation(s) it seeks to elucidate, and to establish its (or their) characteristic properties.

It is well to note that the consequence specification requirement imposes on the theorist no obligation to say anything about *arguments*, at least not in their everyday sense. When the requirement is met, a useful equivalence will have been revealed.  $\Psi$ will be a consequence of  $\Sigma$  if and only if  $\langle \Sigma, \psi \rangle$  is a valid sequence. There is a tradition in logic, beginning with Aristotle, to call structures such as these arguments. But "argument" here is a technical term, whose meaning—if again the Some-camp is right—permits arguments galore which no one ever will, should or could actually *make*. So we should be careful in our talk of arguments.

Consequence-drawing presents the logician with a second major challenge:

The consequence-drawing requirement: Logicians should adjudicate the conflict between the All-camp and the Some-camp; and if they find for the Some-camp, they should specify the conditions under which it is correct and permissible to draw a consequence that  $\sum$  has.

In many ways this is logic's toughest assignment. I have little space for it here, beyond brief mention of some of the thornier issues. The question of when to draw a consequence is conditioned by a number of factors. Computational capacity affects what a drawer is able to do and that in turn depends on the kind of being he (or it) is, what he is built for and what he is good at. Interest also has a bearing. What consequence it makes sense for a drawer to draw or try to draw are those that (he thinks may) answer to his interests, including what at the moment he wants to know. A third factor concerns premiss-management, with a knock-on effect for consequence-drawing. A case in point is premiss-inconsistency. To what extent, if any, should premissinconsistency shape consequence-drawing decisions?

We might note that it is not obvious that logic's traditional tie to argument is any better-nourished by consequence-drawing than consequence-having. Certainly it is true that conclusiondrawing is often implicated in the making of arguments. But it is certainly not true that consequence-drawing requires that an argument be made. Here is why (roughly). Suppose that  $\psi$  is a consequence of  $\Sigma$  and, thinking that the  $\Phi_i$  of  $\Sigma$  are all true, you believe that  $\psi$  is true. For this to be so it is not necessary—or even all that frequent—that you are *making a case* for  $\psi$ . But, in its everyday sense, that's just what argument-making is.<sup>31</sup>

Something like the point I'm after here can be found in the familiar distinction between a *deduction*  $\langle \Phi_1, ..., \Phi_n, \psi \rangle$  and the *derivation* of  $\psi$  from those same hypotheses { $\Phi_1, ..., \Phi_n$ }. The deduction of  $\psi$  from { $\Phi_1, ..., \Phi_n$ } is entirely a matter for the consequence relation. Derivation is different. Deductions are proper parts of derivations. But there is no derivation without justificatory marginalia opposite the lines of the deduction it encompasses. For example, if  $\langle {\Phi, \Phi \supset \psi }, \psi \rangle$  is a deduction, it is not a derivation unless supplemented by the observation that  $\psi$  really does follow from { $\Phi, \Phi \supset \psi$ } by application of the rule *modus tollens*. What happens in the margins is *case-making*. Derivations are argumentative. Deductions are argumentatively inert.

Consequence-having and consequence-drawing are two of a class of C-properties of particular importance for logic. So is the property of premiss-consistency. A fourth C-property is *conditionality*. Here the basic idea is that consequence-having is something that is conditionally expressible; that whenever  $\psi$  is a consequence of  $\{\Phi_1, ..., \Phi_n\}$ , then there are conditions under which  $\exists f \Phi_1 \land \Phi_2, ..., \Phi_n$ , then  $\psi^{\neg}$  is true. Accordingly,

The conditionality of consequence thesis:  $\psi$  is a consequence of  $\{\Phi_1, ..., \Phi_n\}$  if and only if its corresponding conditional is true.

This, if true, encumbers the would-be logician with additional work.

*The conditionality search requirement.* For each consequence relation a logic specifies, it must identify the conditions for an "if ... then"-sentence that make the conditionality of consequence thesis true of it.

A good deal of ink and high-feeling has been spilt over the thesis and the requirement. In the early days, there was an instructive battle between Russell and Hugh MacColl over the horseshoe. Russell thought that there was a relation of material consequence and a sense of "if ... then" for the conditional sentences  $\neg \Phi \supset \psi \neg$  that express it. MacColl thought that there was

<sup>&</sup>lt;sup>31</sup> Relatedly, if we accept Robert Pinto's proposal to regard arguments as invitations to accept (or make) inferences, it takes some tugging and pulling to get it to be the case that every time I draw one of  $\Sigma$ 's consequence, I am inviting someone or other to draw the inference  $\Box$ ,  $\psi$ . See his *Argument, Inference and Dialectic,* Dordrecht and Boston: Kluwer, 2001.

no sense of "if ... then" for which  $\overline{\Phi} \supset \overline{\psi}$  was a conditional sentence. So, if there were a relation of material consequence, the conditionality of entailment thesis wouldn't be true.<sup>32</sup> Mac-Coll's objection anticipated a similar one by C.I. Lewis.<sup>33</sup> Whether or not there are conditions under which  $\overline{\Phi} \supset \overline{\psi}$  is a conditional, and whether or not there is a relation of material consequence which that conditional expresses, material consequence isn't strict (i.e. honest-to-goodness) consequence, and " $\supset$ " doesn't express it. Lewis went on to propose that this omission could be rectified by introducing a new conditional symbol "-3". In effect, he thought that " $\supset$ " fails the conditionality of consequence requirement, and with it the conditionality specification requirement, whereas "-3" satisfies them both.

Was Lewis right about " $\rightarrow$  "? Are the truth conditions he assigned to " $\rightarrow$  "-sentences such as to verify an "if ... then" sentence? Putting " $\Diamond$ " for the possibility operator, Lewis defined " $\rightarrow$ 3" as follows:

 $\Phi \rightarrow \psi$  iff  $\sim \Diamond (\Phi \land \sim \psi)$ .

It is interesting to compare this with the classical definition of " $\supset$ ":

 $\Phi \supset \psi$  iff  $\sim (\Phi \land \sim \psi)$ .

MacColl's point was that the truth of  $\neg (\Phi \land \neg \psi)$  was insufficient for the truth of any sentence in the form If  $\Phi$  then  $\psi$ . Anticipating Lewis' definition, MacColl also thought that there were indeed sentences in the form If  $\Phi$  then  $\psi$  for whose truth the truth of  $\neg \Diamond (\Phi \land \neg \psi)$  is sufficient.

Lewis championed the idea that consequence should be conditionally expressible. Although he didn't say so explicitly, it is evidently his view that

<sup>&</sup>lt;sup>32</sup> See Hugh MacColl, "'If' and 'Imply', *Mind*, 17 (1908), 151-152, and 453-455, Russell, "'If' and 'Imply' a reply to Mr. MacColl," *Mind* 17 (1908), and Russell, "*Review: Symbolic Logic and its Applications*, by Hugh MacColl" *Mind*, 17 (1908). An excellent survey of MacColl's contributions to logic is Shahid Rahman's and Juan Redmond's *Hugh MacColl: An Overview of His Logical Work with Anthology*, London: College Publications, 2007.

<sup>&</sup>lt;sup>33</sup> See, for example, his "Implication and the algebra of logic", *Mind*, 21 (1912), 522-531.

*Sufficiency*: No sentence  $\exists f \Phi \text{ then } \psi^{\exists} \text{ is true unless there}$  is a sense of sufficiency in which the truth of  $\Phi$  is sufficient for the truth of  $\psi^{34}$ 

What might these senses be? The obvious candidates include: Logical sufficiency, mathematical sufficiency, metaphysical sufficiency, causal sufficiency and physical sufficiency. Although they can be set down with a confidence that bespeaks their obviousness, no one should think that the similarities and differences among them have been worked out to everyone's satisfaction. I invoke them here to assist in making a small but hardly trivial point. It is that when it comes to an antecedent's sufficiency for its consequent, there is more than one way to skin that cat, never mind that the complete story has yet to be told.

If the sufficiency claim is right, the conditionality of consequence thesis falls out rather easily. If there is a sense in which  $\Phi$  is sufficient for  $\psi$  then there is a sense in which  $\Box$  if  $\Phi$  then  $\psi$ <sup>-</sup> is true and a sense in which  $\psi$  is a consequence of  $\Phi$  (the same sense throughout).

In footnote 6, I raised the question whether there is a relation of plausible consequence. If there is and the conditionality of consequence thesis is true, the conditionality specification requirement demands that we find conditions under which whenever  $\psi$  is a plausibilistic consequence of  $\Phi$ , there is a true sentence  $\exists f \Phi$  then  $\psi^{\exists}$  in which the truth of  $\Phi$  is in some requisitely distinctive sense sufficient for the truth of  $\psi$ . I confess that I can find no such conditions and no such sense.

Consider a case. Suppose that "There's been a burglary" is a plausibilistic consequence of "The door's been left open and the side-window smashed". Whatever the truth conditions of the plausibilistic-consequence claim, there is no sense of sufficiency for which the truth of "The door's been left open and the sidewindow's been smashed" is sufficient for the truth of "There's been a robbery".

This leaves us with three possibilities. One is that the conditionality of consequence thesis is true and there is no relation of plausibilistic consequence. Another is that there is a relation of plausibilistic consequence and the conditionality of consequence thesis is false. But if that were so, propositions

<sup>&</sup>lt;sup>34</sup> Relevant logicians dispute the sufficiency of  $\neg \diamond (\Phi \land \neg \psi)$  for the entailment of  $\psi$  by  $\Phi$ , and presumably also for the truth of  $\neg$ If  $\Phi$  then  $\psi$ . This is because no relevant logician would accept (except ironically) any sentence in the form  $\neg$ If  $\Phi \land \neg \Phi$ , then  $\psi$  where  $\psi$  is arbitrary. It doesn't matter. Whatever their truth conditions for consequence, their view will also be that for any  $\Phi$  and  $\psi$  that satisfy them,  $\Phi$  will be sufficient for  $\psi$  and  $\neg$ If  $\Phi$  then  $\psi$ will be a true conditional.

could have consequences for whose truth they are insufficient. The same would be true, by the way, for defeasible consequence, nonmonotonic consequence, and, of course, inductive consequence. The third possibility is that there is no relation of plausibilistic consequence independently of whether the conditionality of consequence thesis is true. If this were so, we could say that, whereas the burglary case is an example of *conclusion*-reaching, this is not something that depends on the presence of a *consequence* relation obtaining between the thing concluded and the things concluded from.<sup>35</sup>

The conditionality of consequence thesis receives what perhaps its strongest theoretical support from the large family of deductive logics for which a deduction metatheorem is provable. As applied to first order classical logic, there is a case of it that appears to conform to the conditionality of consequence thesis, virtually word for word.

Deduction metatheorem:  $\psi$  is a semantic consequence of  $\Phi$  if and only if  $\overline{\Phi} \supset \psi$  is a semantically valid sentence.

However, it is known that there is no full deduction metatheorem for certain classes of logics of (what logicians take to be) defeasible consequence.<sup>36</sup> For some logicians the lack of a deduction metatheorem is a deal-breaker. Perhaps it is. This is something we will have to make up our minds about. If indeed it is a deal-breaker, then for the class of cases in question there is no relation of defeasible consequence, and, if the consequence search requirement is sound, no logic of defeasible reasoning either. If it is not a deal-breaker, the entrenched idea that what consequences are consequences of are propositions sufficient for their truth will have to be dug up and discarded.

#### 5. Inductive consequence

This is the place where I want to get to the bottom of Hamblin's D—the property that deduction has and induction lacks, in virtue of which it may be doubted induction is logic-worthy.

It is no slander to say that logicians who honour the consequence specification requirement and who cleave to the consequence dependency of conclusion-drawing are hard-heads

<sup>&</sup>lt;sup>35</sup> This is the position of my *Seductions and Shortcuts: Error in the Cognitive Economy*, scheduled to appear in 2012 or early 2013.

<sup>&</sup>lt;sup>36</sup> Charles Morgan, "The nature of nonmonotonic reasoning", *Minds and Machines*, 10 (2000) 321-360.

about what to count as logic. Their heads are even harder if their loyalties also extend to the conditionality of consequence thesis. If the loyalties are justified, a great deal of what passes for logic these days isn't. A good question is: If these principles are sound, how far does the disestablishment of logic go? Does it, for example, cause trouble for the logic of induction? Does it cause trouble for induction in a way that sheds light on Hamblin's dark sayings about it in *Fallacies*?

There is a common and long-held view according to which  $\psi$  is an *inductive consequence* of  $\{\Phi_1, \ldots, \Phi_n\}$  if (and on some tellings only if<sup>37</sup>), the conditional probability of  $\psi$  on  $[\Phi_1 \land \ldots \land \Phi_n]$  is sufficiently high. Perhaps this is right. For a certain large class of inductive reasonings, I think it is right. Think here of statistico-experimental reasoning. If it is, it is so notwithstanding that the truth of the  $\Phi_i$  are not sufficient for the truth of  $\psi$ , and, correlatively, that the conditional probability at hand is not such as to license  $[If \Phi_1 \land \ldots \land \Phi_n]$ , then  $\psi$ . But, right or wrong, there is a further question to put. It is the question whether the relations of *lending support to or being evidence for* can obtain between  $[\Phi_1 \land \ldots \land \Phi_n]$  and  $\psi$  without its also being the case that  $\psi$  is, in the sense at hand, an inductive consequence of the  $\Phi_i$ . Of course, it depends on whether we're prepared to hold inductive consequence to a sufficiency condition of its own:

Sufficiency\*:  $\psi$  is an inductive consequence of { $\Phi_1$ , ...,  $\Phi_n$ } only if there is some sense of sufficiency in which the truth of  $\overline{\Phi_1} \wedge \ldots \wedge \Phi_n$  is sufficient for the truth of  $\psi$ .

Here, too, opinion is divided: One way in which sufficiency<sup>\*</sup> could fail would be where  $\psi$  is rightly concluded from evidence that supports it, notwithstanding that  $\psi$  is not a consequence of it. I myself am of that view. That is not what matters here. What matters here is whether it is *Hamblin*'s view, or whether, had he had occasion to reflect upon it, it would have been. Let us suppose so. How would this bear upon the question of whether there is a logic for inductive reasoning? It would bear, or not, depending on whether Hamblin would also accept the consequence specification requirement: No consequence relation, no logic. Period.

<sup>&</sup>lt;sup>37</sup> I myself am not in the only-if camp. Consider a case. You are tramping in the wilds of Brazil and your companion points out an ocelot. It is your first ocelot. "How interesting", you exclaim, "I always imagined that ocelots would be two-legged, not four!" I think that this is a competent induction, for a realistically broad notion of induction. But judged by, say, Bayesian standards, it's a train wreck.

I think it may fairly be surmised that Hamblin's feature D, in whose absence a logic is not possible and in whose presence the opposite is true is *satisfaction of the consequence specification requirement*. Deduction satisfies it. Induction—for the class of cases in view—may not, and Hamblin himself appears to think that it does not. How so?

Hamblin wonders whether inductive arguments are really arguments. That bears repeating: *He wonders whether inductive arguments are really arguments*. It is an astonishing claim, made even more so by his acknowledgement that we sometimes make probabilistic arguments, writing that

... no one is going to be much interested in probabilistic argument unless the probability of the premisses very clearly outweighs the *a priori* improbability of the conclusion. (240)

Even so, although calling inductive arguments 'arguments' is

to mark a similarity to deductive arguments ... it might be as well to reassure ourselves that the similarities are really as great as the differences. (226)

Earlier I expressed surprise that Hamblin should be a sceptic about inductive logic in the face of burgeoning work on probability. How, I suggested, could Hamblin not have been aware that probability theory was, if not all of inductive logic, then its theoretical core? How could he not know of the vital alliance between induction and probabilistic reasoning?

If we look closely at the passages quoted, we see a readiness on Hamblin's part to distrust this partnership—cutting some slack to probabilistic argument and hardly any to inductive argument. My present conjecture is that Hamblin's hostility to inductive logic stems from its lack of a bona fide consequence relation. I now conjecture that his further view is that reasoning probabilistically isn't consequence-drawing either. This being so, probability cannot overcome the deficiency that makes for the logic-unworthiness of induction. In plain words:

*No matter the details, we can't get a logic of induction from probability theory.* 

This, if true, is something to pay attention to. So let's look into this a bit further.

#### 6. Saving inductive consequence?

Not surprisingly, inductive logics brim with attempts to hang on to the idea of inductive consequence in a systematic way. Here is Jon Williamson on this point, speaking for, as they are called, logical theories of probability:

Perhaps the most obvious thing to try first is a generalization of entailment  $\models$  to partial entailment  $\models_x$ , where a set  $\Theta$  of sentences partially entails sentence  $\Phi$  to degree x,  $\Theta \models_x \Phi$ , if and only if  $p(\Phi \land \Theta) = x$ . Under such a view classical entailment is the case where x = 1. If  $\Theta$  is empty we get a concept of degree of logical truth which corresponds to unconditional probability.<sup>38</sup>

Of course, partial entailment gives partial consequence. My view is that partial consequence is consequence in name only. Partial consequence fails sufficiency\*.

Perhaps there is another way of getting inductive consequence back into gainful employment. Suppose, as before, we grounded inductive consequence in conditional probability, which on the conjecture just above is precisely what Hamblin would deny. Suppose, even so, that whenever  $p(\Phi \land \Theta) \ge n$ , for some suitable value of n, we would have it that

(1) If  $\Theta$ , then *probably* ( $\Phi$ )

and with it that

 $(1') \Phi$  is an inductive consequence of  $\Theta$ .

This provides a key contrast between the partial consequence relation of logical theorists of probability and—as we have it here—inductive consequence. The difference is what happens *in the interior* of the corresponding conditional sentences. In the case of partial consequence, the conditional is

(2) If  $\Theta$ , then  $\Phi$ .

But (2) differs from (1) essentially. The consequence of (1) arises from the consequent of (2) by prefixation of the sentence operator "probably" to (2)'s consequent. If we think (2) false and (1) true in virtue of "probably"'s respective absence and presence, there is a way now of producing the conditional corresponding to partial consequence. We simply *rewrite* (2) as (1).

<sup>&</sup>lt;sup>38</sup> "Probability logic", in Gabbay *et al., Handbook of the Logic of Argument and Inference*, pages 397-424; p. 404.

The difference with Hamblin is now clearly discernible. He writes,

The logician commonly conceives arguments on the pattern 'P, therefore Q'; but ... we do not normally say 'This crow is black; that crow is black; therefore all crows are black'. ... Instead, we frame, *at most*, a modified conclusion in the form, 'Therefore it is a reasonable conclusion that ...', or 'So probably ...', or 'So presumably.' (p. 226)

There it is in a nutshell. Expressions in the form  $\Theta$ , therefore  $\Phi^{\neg}$  encode genuine arguments and are genuinely logic-worthy. Expressions in the form  $\Theta$ , therefore probably  $\Phi^{\neg}$  encode what are sometimes called arguments and thus give the impression of logic-worthiness. But the impression is wrong.

Similarly, the right interpretation of "if ... then" in

If  $\Theta$ , then  $\Phi$ 

gives consequence, whereas in

If  $\Theta$ , then probably ( $\Phi$ )

it does not.

It is an interesting test, about as hard-headed as they come. Not only does it put inductive logic out of business; it upends the whole family of defeasibility and default logics.

Apart from Hamblin's opinion of it, the present suggestion for generating consequence relations is interesting in its own right and, as I say, interesting enough to stay with a while longer.

## 7. Plausibilistic consequence?

There is no greater force driving logic's pluralism than the variety and sheer number of its consequence relations, real or imagined. *Pace* Hamblin, our rescue, just now, of inductive consequence may suggest itself as a model for the other contenders, the very ones on which we were inclined to give up on only brief sections ago—plausibilistic consequence, defeasiblistic consequence, nonmonotonic consequence, presumptive consequence, the lot. In the space remaining to me, I will consider only the plausibility case. For this to work, we will need sentences in the form

## (3) If $\Theta$ , then plausibly ( $\Phi$ )

that meet the requisite grounding condition. And for that to wash, there must already exist, or be concurrently producible, a sufficient theoretical grasp of sentences in the form plausibly  $(\Phi)$  as they occur in probabilistic conditionals If  $\Theta$  then probably  $(\Phi)$ , to motivate whatever is proposed as their ground. In the case of If  $\Theta$  then probably  $(\Phi)$ , we saw a grounding link in the conditional probability of  $\Phi$ , and we proposed that if the conditional probability of  $\Phi$  on  $\Theta$  is high enough,  $\Theta$  may serve as antecedent in a true sufficiency conditional whose consequent is probably  $(\Phi)$ . That linkage constitutes the ground of (1), If  $\Theta$  then probably  $(\Phi)$ . We can say the same thing more briefly:

*Grounding inductive consequence: Pace* Hamblin, inductive consequence is grounded in a *probability logic*.

The question is whether there exists a like grounding for  $[plausibly (\Phi)]$  as it occurs in  $[If \Theta]$  then plausibly  $(\Phi)$ . Do sentences like (3) meet a grounding condition in the manner of (1)? Have we got a *plausibility logic*? Might there be a relation of *conditional plausibility*, and might it be analytically exploitable in the manner of conditional probability?

There are some interesting writings on plausibility, of which the best to date by a logician is Nicholas Rescher's *Plausible Reasoning* published in Assen by van Gorcum in 1976.<sup>39</sup> Plausibility is unruly. It behaves very differently from probability. As mentioned in footnote 6, it has no stable concept of negation. A given body of evidence can make incompatible propositions equally plausible, with obvious implications for closure under conjunction. Certainly there are logicians for whom the following refrain is decisive: *No negation, no logic*!

On the other hand, one of the better treatments by computer scientists, Nir Frieman's and Joseph Halpern's theory of plausibility measures, is a low-structure generalization of probability. Plausibility is a partially ordered relation subject to a distinguishing axiom that says that a set of sentences must be at least as plausible as any of its subsets. Addition of two further axioms gives the so-called KLM properties for default logic. The first of this pair provides that if (i) A, B and C are pairwise disjoint sets, (ii) the plausibility of  $A \cup B$  exceeds that of C, and (iii) the plausibility of  $A \cup C$  exceeds that of B, then the plausi-

<sup>&</sup>lt;sup>39</sup> For some thoughts of my own, see Gabbay's and my *The Reach of Abduction: Insight and Trial*, Amsterdam: North Holland, 2005; Chapter 7. For a different perspective, Walton's *Plausible Argument in Everyday Conversation*. Albany, NY: SUNY Press, 1992.

bility of A alone exceeds the plausibility of  $B \cup C$ . The other axiom stipulates that if A and B are both utterly implausible, so is  $A \cup B$ . The KLM properties of a putative default conditional  $\rightarrow$  are set by a reflexivity axiom, and the rules of left logical consequence, right weakening, conjunction, disjunction and cautious monotonicity.<sup>40</sup>

An important feature of plausibility measures is that the spaces they measure are direct generalizations of probability spaces. This gives rise to a notion of conditional plausibility analogous to what is required for Bayesian networks. The question is whether conditional plausibility is grounding in the required way. Putting "pl" for "plausibly", does  $Pl(\Phi \land \Theta) = x$  ground a sufficiency conditional,  $If \Theta$  then  $pl(\Phi)$ , when *x* is big enough? If so, wouldn't plausibilistic consequence be back in business? Notwithstanding the weakness of some of the KLM properties,<sup>41</sup> it would seem—against Hamblin—that it might.

In a good deal of the plausibility literature there is also a tendency to *pragmaticize* plausibility. This is fine with me. Sometimes "plausible" is a hedge. Sometimes its function is a matter of context, including who's saying what to whom. Sometimes, in short, "That's plausible" is a *commitment*-qualifier. But that is not what we are after at present. We are after a relation that qualifies  $\psi$  as a plausible *consequence* of  $\Theta$ . Our quest is semantic.

We were seeking a relation between  $\Theta$  and  $\Phi$  in virtue of which  $\Theta$  would be sufficient for plausibly  $(\Phi)^{-1}$ . If our search paid off, we could say that  $\Phi$  is a plausibilistic consequence of  $\Theta$ . Perhaps it is the same with those other consequence relations that pullulate in the stipulations of an ever-expanding literature. If so, there will be a relation between  $\Theta$  and  $\Phi$  in virtue of which

<sup>&</sup>lt;sup>40</sup> The KLM properties are named after their proposers: S. Kraus, D. Lehmann and M. Magidor, "Nonmonotonic reasoning, preferential models, and cumululative logics", *Artificial Intyelligence*, 44 (1990), 167-207. For plausibility measures, see Nir Friedman and Joseph Y. Halpern, "Plausibility measures: A user's guide", *Proceedings of the Eleventh Conference on Uncertainty in AI*, 1995, 175-184, and "Plausibility measures and default reasoning", N. Friedman and J. Halpern "Plausibility measures and default reasoning", *Journal of the ACM* 48 (1996), 1297-1304. As for the KLM properties: Reflexivity provides that  $\Phi \rightarrow \Phi$ . Left logical equivalence is: If  $\vdash \Phi \Leftrightarrow$  $\Phi'$ , then from  $\neg \Phi \rightarrow \psi$  infer  $\neg \Phi' \rightarrow \psi$ . Right weakening is: If  $\psi \Rightarrow \psi'$ , then from  $\neg \Phi \rightarrow \psi$  infer  $\neg \Phi' \rightarrow \psi'$ . Conjunction is: From  $\neg \Phi \rightarrow \psi_1$  and  $\neg \Phi \rightarrow \psi_2$ infer  $\neg \Phi \rightarrow (\psi_1 \land \psi_2)$ . Disjunction is: From  $\neg \Phi \rightarrow \psi_1$  and  $\neg \Phi \rightarrow \psi_2$ infer  $\neg (\Phi \land \psi_2) \rightarrow \psi$ . Cautious monotonicity is: From  $\neg \Phi \rightarrow \psi_1$  and  $\neg \Phi \rightarrow \psi_2$ infer  $\neg (\Phi \land \psi_2) \rightarrow \psi_1$ .

<sup>&</sup>lt;sup>41</sup> For example, reflexivity fails intuitively; no proposition is a *default* consequence of itself. Moreover, if we allow that if  $\models \psi$  then  $\Phi \models \psi$ , then we have the paradox of necessity for  $\rightarrow$ , and likewise for right weakening.

if  $\Theta$  then *defeasibly* ( $\Phi$ ), and a possibly different relation between  $\Theta$  and  $\Phi$  such that if  $\Theta$  then *presumably* ( $\Phi$ ), and a relation such that if  $\Theta$  then *autoepistemically* ( $\Phi$ ); and so on. This, it seems to me, is one of the most important open questions in modern logical theory. No one doubts that the logic and computer science literatures abound in consequence purporting *names*—"defeasible consequence", "default consequence", "autoepistemic consequence", and whatever else. No one doubts the names. But there is room to wonder about the putative nominata. There is room for doubt whether we have achieved a rescue of plausibilistic consequence. The same doubt—and more—applies to the like rescue of the others.

A last word about plausibility. If it exists, I haven't much of a general idea of how to parse the relation between  $\Theta$  and  $\Phi$  in virtue of which

(3) If  $\Theta$ , then plausibly ( $\Phi$ )

is true. But, returning briefly to the burglary example, I have no hesitation in accepting as true

(4) If the door was left open and the side-window was smashed, then plausibly (there's been a burglary).

That is, I have no hesitation is supposing that (4) meets the sufficiency requirement for conditionality. If this is so, then the queried relation between  $\Theta$  and  $\Phi$  exists, and nothing precludes our calling it plausibilistic consequence in this case:

(5) That there's been a burglary is a plausibilistic consequence of the door's having been left open and the side-window's having been smashed.

But here is a point to give us pause. We see in the interplay between (4) and (5) that it is (4) that wears the trousers. All I mean by this is that for a reflectively competent speaker of English it is a more untutoredly accessible matter to determine whether (4) is true and—independently of that—a barely accessible matter to determine whether (5) is true. (Who, without tuition, knows what plausibilistic consequence is supposed to be?)

It is the same way, I should have thought, with presumptive consequence (after all "presumably" is untutoredly accessible), but perhaps not with, say, nonmonotonic or autoepistemic consequence, whose cognate sentence-adverbs are not accessible without instruction.

Be that as it may, the literature on defeasibility and monotonicity, and their numerous variations and adaptations, is

too big for anyone to read in even a generously proportioned lifetime. But surely, it will be said, there are manageable families of such logics, many well-known and some classics, in which the requisite consequence relations have long since been well catered for. How, then, can there be any question as to the existence and *bona fides* of, say, defeasible consequence and nonmonotonic consequence? I have two things to say about this. One (I repeat myself) is that calling something a defeasible consequence relation doesn't make it the case that *any* consequence relation is actually it. The other is that if these purported logics shed light enough on "defeasibly" (etc.) to enable the grounding of sufficiency conditionals of the form  $\exists F \Theta$ , then defeasibly (etc.)  $\Phi^{\neg}$ , then the logics of defeasible (etc.) consequence, are fully deserving of the name (each time).<sup>42</sup>

## 8. Conclusion

Hamblin is a hard-head about induction. He has difficulty in seeing how inductive arguments can actually be arguments. He notices that you can't get an unqualified sufficiency conditional from the fact that the conditional probability of  $\Phi$  on  $\Theta$  is very high. He makes too much of this. He thinks that a logic of induction can't be got from a logic of probability. He thinks that a logic of induction can't be got at all. This makes for a sweeping scepticism. Since there is no logic for induction, there is no logic for the inductive fallacies. A fallacy is an inapparently bad argument; but since it is not apparent that there *are* any inductive arguments, it is not apparent that there are any inductive *fallacies*.

Sweeping as it is, how could this scepticism not also carry in its path the dialogue logics that have proliferated these past four decades? The short answer is: It depends on the nature of the arguments that a logic purports to model. If it models discourse in which inductive reasoning occurs, then it is not a logic. At least, it is not a logic by the largely undeveloped lights of Hamblin's chapters 1 and 7. It is an odd conclusion. It makes one want to go through chapters 7 and 8 with a fine-tooth comb. It makes one think how long ago was the fateful year 1970.<sup>43</sup>

<sup>&</sup>lt;sup>42</sup> I myself think that the K-consequence principle is false, a minority claim I develop in *Seductions and Shortcuts*. As is argued there, there are types of disciplined and assessable reasoning for which no distinctive consequence relation is definable. Saying why is a long story, much beyond what we have space for here. <sup>43</sup> For helpful compared to a set of the set o

<sup>&</sup>lt;sup>43</sup> For helpful comments on earlier drafts I warmly thank Peter Bruza, Maurice Finocchiaro, David Hitchcock, Lorenzo Magnani, Fabio Paglieri, Alirio Rosales and Harvey Siegel. For stimulating discussions about

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