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# Design Feed Forward Neural Network to Determine Doses of the Decongestant for Cold Pills 

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#### Abstract

The aim of this paper is to design feed forward neural network to determine the effects of cold pills and cascades from simulation the problem to system of first order initial value problem. This problem is typical of the many models of the passage of medication throughout the body. Designer model is an important part of the process by which dosage levels are set. A critical factor is the need to keep the levels of medication high enough to be effective, but not so high that they are dangerous.


Keyword: Ann, feed forward neural network, propagation training algorithm.

## Introduction

The study of cold pills based on the work of the contemporary applied mathematician, Edward Spitznagel Professor of Mathematics at Washington University, St. Louis, Missouri [1]. In this paper we design feed forward neural network(FFNN) to determine the doses of decongestant since FFNNs are parallel computational models comprised of densely interconnected, simple, adaptive processing units, characterized by an inherent propensity for storing experiential knowledge and rendering it available for use, FFNNs resemble the human brain in two fundamental respects; Firstly, knowledge is acquired by the network from its environment through a learning process, and secondly, interneuron connection strengths, known as synaptic weights are employed to store the acquired knowledge[2]. In the proposed approach the model function is expressed as the sum of two terms: the first term satisfies the initial conditions (IC) and contains no adjustable parameters. The second term can be found by using feed forward neural network(FFNN) which is trained so as to satisfy the differential equation and such technique is called collocation neural network. Since it is known that a multilayer FFNN with one hidden layer can approximate any function to arbitrary accuracy [3],[4] thus our FFNN contains one hidden layer. Now, we illustrate how our approach can be used to find the approximate solution of the system of first order differential equation:
$y_{i}^{\prime}(\mathrm{x})=\mathrm{F}_{\mathrm{i}}\left(\mathrm{x}, \mathrm{y}_{1}, \mathrm{y}_{2}\right), \quad \mathrm{i}=1,2 \quad$, (1)
where a subject to certain IC's and $x \in R, D \subset R^{n}$ denotes the domain and $y(x)$ is the solution to be computed.

If $y_{t}(x, p)$ denotes a trial solution with adjustable parameters $p$, the problem is transformed to a discretize form:
$\operatorname{Min}_{\mathrm{p}} \sum_{\vec{x}_{\mathrm{i}} \in \hat{\mathrm{D}}} \mathrm{F}\left(\mathrm{x}_{\mathrm{i}}, \mathrm{y}_{\mathrm{t} 1}\left(\mathrm{x}_{\mathrm{i}}, \mathrm{p}\right), \mathrm{y}_{\mathrm{t} 2}\left(\mathrm{x}_{\mathrm{i}}, \mathrm{p}\right)\right) \quad$,
subject to the constraints imposed by the IC's.
In the proposed approach, the trial solution $y_{t}$ employs a FFNN and the parameters $p$ correspond to the weights and biases of the neural architecture. We choose a form for the trial

function $\mathrm{y}_{\mathrm{t}}(\mathrm{x})$ such that it satisfies the IC's. This is achieved by writing it as a sum of two terms:

$$
\begin{equation*}
y_{t}\left(x_{i}, p\right)=A(x)+G(x, N(x, p)) \tag{3}
\end{equation*}
$$

where $N(x, p)$ is a single output FFNN with parameters $p$ and $n$ input units fed with the input vector x . The term $\mathrm{A}(\mathrm{x})$ contains no adjustable parameters and satisfies the IC's. The second term G is constructed so as not to contribute to the IC's, since $\mathrm{y}_{\mathrm{t}}(\mathrm{x})$ satisfy them. This term can be formed by using a FFNN whose weights and biases are to be adjusted in order to deal with the minimization problem.

## Computation of the Gradient

An efficient minimization of (2) can be considered as a procedure of training the FFNN, where the error corresponding to each input vector $\mathrm{x}_{\mathrm{i}}$ is the value $\mathrm{E}\left(\mathrm{x}_{\mathrm{i}}\right)$ which has to force near zero. Computation of this error value involves not only the FFNN output but also the derivatives of the output with respect to any of its inputs. Therefore, in computing the gradient of the error with respect to the network weights consider a multi layer FFNN with n input units (where $n$ is the dimensions of the domain) one hidden layer with H sigmoid units and a linear output unit.
For a given input vector $\mathrm{x}=\left(\mathrm{x}_{1}, \mathrm{x}_{2}, \ldots, \mathrm{x}_{\mathrm{n}}\right)$ the output of the FFNN is :

$$
\mathrm{N}=\sum_{\mathrm{i}=1}^{\mathrm{H}} v_{\mathrm{i}} \sigma\left(\mathrm{z}_{\mathrm{i}}\right) \text {, where } \mathrm{z}_{\mathrm{i}}=\sum_{\mathrm{j}=1}^{\mathrm{n}} \mathrm{w}_{\mathrm{ij}} \mathrm{x}_{\mathrm{j}}+\mathrm{b}_{\mathrm{i}}
$$

$\mathrm{w}_{\mathrm{ij}}$ denotes the weight connecting the input unit j to the hidden unit i
$v_{\mathrm{i}}$ denotes the weight connecting the hidden unit i to the out put unit ,
$b_{i}$ denotes the bias of hidden unit $i$, and
$\sigma(z)$ is the sigmoid transfer function ( tanhsig. ).
The gradient of FFNN, with respect to the parameters of the FFNN can be easily obtained as:

$$
\begin{align*}
& \frac{\partial \mathrm{N}}{\partial v_{\mathrm{i}}}=\sigma\left(\mathrm{z}_{\mathrm{i}}\right)  \tag{4}\\
& \frac{\partial \mathbf{N}}{\partial \mathbf{b}_{\mathrm{i}}}=v_{\mathrm{i}} \sigma^{\prime}\left(\mathrm{z}_{\mathrm{i}}\right)  \tag{5}\\
& \frac{\partial \mathrm{N}}{\partial \mathrm{w}_{\mathrm{ij}}}=v_{\mathrm{i}} \sigma^{\prime}\left(\mathrm{z}_{\mathrm{i}}\right) \mathrm{x}_{\mathrm{j}} \tag{6}
\end{align*}
$$

Once the derivative of the error with respect to the network parameters has been defined, then it is a straight forward to employ any minimization technique. It must also be noted, the batch mode of weight updates may be employed.

## Cold Pills and Cascades

At the first sign of a cold many of us start to take cold pills. These pills usually contain a decongestant to relieve stuffiness. The pill dissolves in the gastrointestinal tract, and the two medications diffuse into the bloodstream. The bloodstream takes the medications to the sites where they have therapeutic effect. Both medications are eventually removed from the blood by the kidneys and the liver. The dynamics of the rising and falling levels of the medications in the GI tract and in the bloodstream may be modeled by system of first-order linear differential equations. Pharmaceutical companies do extensive testing to determine the movement medications through the body. This process is modeled by treating various components of the human body as compartments and following the medication as it enters and leaves these compartments. Examples of body compartments are the GI tract, the bloodstream, the tissues and the excretory system. Testing has shown that a typical cold medication leaves one compartment (e.g., the GI tract) and moves into another (e.g., the bloodstream) at a rate proportional to the amount present in the first compartment. The

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coefficient of proportionality depends upon the specific medication, the compartments involved, and the age and general health of the individual. In this section we look at three models based on different dosage strategies suppose that a single dose of a fast-dissolving cold pill is taken. The pill dissolves "instantaneously" in the GI tract and releases A milligrams of decongestant. Each medication independently diffuses into the bloodstream.

## One Instantly Dissolving Dose: The Model IVP

Let $y_{1}(t)$ be the amount of medicine of decongestant in the GI tract at time $t$ after the pill has dissolved. We shall use the Balance Law to compute the rate of change of the amount in each compartment. Because the medication moves out of the GI tract and into the blood-stream at a rate proportional to the amount in the GI tract, and because nothing is coming in, we have that:

$$
\frac{d y_{1}(t)}{d t}=-k_{1} y_{1}(t), \quad y_{1}(0)=A
$$

where $\mathrm{k}_{1}>0$ is the coefficient of proportionality, and A is the initial amount the units for the rate constant $\mathrm{k}_{1}$ are reciprocals of the units chosen to measure the time $t$. For example the units of $k_{1}$ are (hours) ${ }^{-1}$ if time is given in hours.

The level of medication in the bloodstream will build up from zero (initially, there are no cold medications in the blood), but then will fall as the kidneys and liver do their job of removing "foreign" substances from the blood. If $\mathrm{y}_{2}(\mathrm{t})$ denotes the amount of medication in the bloodstream at time t , then the Balance Law implies that:

$$
\frac{d y_{2}(t)}{d t}=k_{1} y_{1}(t)-k_{2} y_{2}(t), \quad y_{2}(0)=0
$$

The first term on the right side of the rate equation models the observed fact that the medication leaving the GI tract goes directly into the bloodstream ; the second rate term models the clearance of medication from the blood and into the excretory system.
Consequently, the system of first-order ODEs and flow of medication is given by the IVP :

$$
\begin{align*}
& \frac{d y_{1}}{d t}=-k_{1} y_{1} \quad, \quad y_{1}(0)=A \\
& \frac{d y_{2}}{d t}=k_{1} y_{1}-k_{2} y_{2}, \quad y_{2}(0)=0 \tag{7}
\end{align*}
$$

where the (positive) coefficient $\mathrm{k}_{2}$ is typically smaller than $\mathrm{k}_{1}$.
System (7) models the flow of decongestant. However, the flow rates differ because the experimentally determined values of the rate constants $\mathrm{k}_{1}$ and $\mathrm{k}_{2}$ are quite different for the two medications (see Table 1). These differences lead to very different levels of the two medications in the bloodstream.
Observe from table (1) how much smaller $\mathrm{k}_{2}$ is than $\mathrm{k}_{1}$. Consequently, the medication will stay in the bloodstream longer than in the GI tract.

## Solving The Model IVP

Professor Edward Spitznagel in [1] solved this problem analytically and obtain the following solution for $k_{1} \neq k_{2}$ :

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$$
\begin{equation*}
y_{1}(t)=A e^{-k_{1} t} \quad, \quad y_{2}(t)=\frac{k_{1} A}{k_{1}-k_{2}}\left(e^{-k_{2} t}-e^{-k_{1} t}\right) \tag{8}
\end{equation*}
$$

where time $t$ is measured forward from the instant the initial dose of A units of medication is released into the GI tract.
From the solution set (8) see that, as expected, the levels of the medication in the GI tract and the bloodstream tend to zero as time increases. Since, the medication is initially at the zero level in the bloodstream, these levels reach a maximum value at some later time.

Now, we solve system(7) for $\mathrm{A}=1$ where $\mathrm{k}_{1}=1.386, \mathrm{k}_{2}=0.1386$ using three layers feed forward neural network with back propagation training algorithm having one input unit, five hidden units with tanhsig. transfer function and one linear output unit. Table (2) gives the analytic and neural solutions with different training algorithm such as : Levenberg Marquardt ( trainlm ) [5], and quasi - Newton (trainbfg)[6] and its errors given in table (3), table(4) gives the weight and bias of the designer network and table(5) gives the performance of the train with epoch and time
Figures (1) show the levels of decongestant in the GI tract and the blood over a six-hour period if the values of $\mathrm{k}_{1}$ and $\mathrm{k}_{2}$ given in Table (1) are used and $\mathrm{A}=1$.
The clearance coefficient $\mathrm{k}_{2}$ of medication from the blood-stream is often much lower for old and sick people than it is for the young and healthy. This means that for some people the medication levels in the blood may become dangerously high even with a "standard" dosage.
Few of us stop with taking one cold pill. The models that follow heat the more realistic setting of taking medication over a period of time.

## Continuous Doses

If a medication is embedded in resins that dissolve at varying rates, a fixed flow of medication can be assured. Tiny beads of the mixture are packed into a capsule, and the medications are released at a constant rate into the CI I tract over a period of hours. One capsule of continuous-acting medication such as CONTAC (Smith-Kline Beecham) may need to be taken only twice a day. The mathematical model for this situation is slightly different from IVP (7). There is no medication in the GI tract at the start of the continuous dosage regimen, but instead there is a constant inflow rate I due to the gradually dissolving beads.

## Continuous-Acting Capsules: Model IVP and its Solution

The model IVP for the amounts $y_{1}(t) a n d y_{2}(t)$ of continuous-acting medication in the GI tract and bloodstream, respectively, is :

$$
\begin{array}{ll}
\frac{d y_{1}}{d t}=I-k_{1} y_{1} \quad, & y_{1}(0)=0 \\
\frac{d y_{2}}{d t}=k_{1} y_{1}-k_{2} y_{2}, & y_{2}(0)=0 \tag{9}
\end{array}
$$

Where I is a positive constant modeling the rate of release of each medication into the GI tract
The system of IVP (9) solved analytically by Professor Edward Spitznagel in [1] and he found the following solution :

$$
\begin{align*}
& y_{1}(t)=\frac{I}{k_{1}}\left(1-e^{-k_{1} t}\right) \\
& y_{2}(t)=\frac{I}{k_{2}}\left[1+\frac{1}{k_{1}-k_{2}}\left(k_{2} e^{-k_{1} t}-k_{1} e^{-k_{2} t}\right)\right] \tag{10}
\end{align*}
$$

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Observe that as time increases, the level of medication in the GI tract tends to I / $\mathrm{k}_{1}$ and that in the bloodstream to I/ $\mathrm{k}_{2}$. The solution formulas (10) are valid for any positive values of the coefficients $\mathrm{k}_{1}$ and $\mathrm{k}_{2}, \mathrm{k}_{1} \neq \mathrm{k}_{2}$.
Now, we solve system (9) where $\mathrm{k}_{1}=1.386, \mathrm{k}_{2}=0.1386$ and $\mathrm{I}=12$, using FFNN .
Table (6) gives the analytic and neural solutions with different training algorithm such as: Levenberg-Marquardt (trainlm), and quasi-Newton (trainbfg) and its errors given in table (7), table(8) gives the weight and bias of the designer network and table(9) gives the performance of the train with epoch and time.

Suppose that the input rate I is taken to be one unit of each medication per hour. Thus, a total dose of twenty-four units is administered continuously over a period of one day. Figures (2) show that, if the values of $k_{1}$ and $k_{2}$ from Table (1) are used, the decongestant builds up quite rapidly to its equilibrium level in the blood.

## Repeated Doses of Fast-Dissolving Pills

Many cold pills dissolve fairly quickly in the GI tract, releasing their medications over a period of no more than half an hour. Repeated doses must then be taken every four to six hours in order to keep up the medication levels in the blood. In this case, the input rate I into the GI tract is not constant, but operates at a high level for a short time, then cuts off entirely until the next dose is taken four to six hours later.

## One Dose livery Six Hours: The Model IVP

In contrast to a continuous acting medication, other forms of medications dissolve very rapidly in the GI tract. This means that the medication is delivered at a high constant rate but only over a short time. Suppose that the rate is 12 units / hour, but delivered in half an hour and then repeated at six-hour intervals. The model IVP is given below:
$\frac{d y_{1}}{d t}=I(t)-k_{1} y_{1}, \quad y_{1}(0)=0$
$\frac{d y_{2}}{d t}=k_{1} y_{1}-k_{2} y_{2}, \quad y_{2}(0)=0$
$I(t)=12 \operatorname{sqw}(t, 12 / 100,6)$
where sqw ( $\mathrm{t}, 12 / 100,6$ ) denotes the pulse function with period 6 hours, which is "on" for half an hour at the start of each period and " off " otherwise ( $1 / 2$ hour $=12 / 100 \%$ of the 6 hour period ). See [7] for a description of sqw and other piecewise continuous functions.

The total dosage of 24 units in one day is the same as in the continuous- acting model .Figures 2 display the medication levels corresponding to this repeated on-off dosage pattern over a forty - eight hour period if values of $\mathrm{k}_{1}$ and $\mathrm{k}_{2}$ are taken from Table 1, using FFNN. Medication levels rise during the half hour the cold pill is dissolving in the GI tract, but then fall until the next dose. The amount of decongestant in the blood quickly reaches and then oscillates around an equilibrium level.

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Tabel (1) : Rate Coefficients of Decongestant for Cold Medications

$$
\begin{array}{ll}
\mathrm{k}_{1} & 1.386 \text { hour }^{-1} \\
\mathrm{k}_{2} & 0.1386 \text { hour }^{-1}
\end{array}
$$

Table (2):The analytic \& neural result of the problem (7)

| $\mathbf{x}$ | Analytic $\left(\mathbf{y}_{\mathbf{1 a}}\right)$ <br> solution | Neural solution <br> (Trainlm) $\left(\mathbf{y}_{\mathbf{1 t}}\right)$ | Neural solution <br> (Trainbfg $)\left(\mathbf{y}_{\mathbf{1 t 2}}\right)$ |
| :---: | :---: | :---: | :---: |
| 0 | 1 | 1 | 0.999837751002654 |
| 0.1 | 0.870576189297161 | 0.870645179547517 | 0.870576189297933 |
| 0.2 | 0.757902901371166 | 0.757902901371166 | 0.757902901371998 |
| 0.3 | 0.659812219732971 | 0.659812219732971 | 0.659810076684370 |
| 0.4 | 0.574416807906831 | 0.574424576246922 | 0.574416254623237 |
| 0.5 | 0.500073595695768 | 0.500073595695768 | 0.500073595698388 |
| 0.6 | 0.435352165308950 | 0.435344727835639 | 0.435352165307395 |
| 0.7 | 0.379007229076934 | 0.379002100324034 | 0.379007285987416 |
| 0.8 | 0.329954669205873 | 0.329954669205873 | 0.329954669210264 |
| 0.9 | 0.287250678558054 | 0.287250678558054 | 0.287250678555912 |
| 1 | 0.250073601112094 | 0.250073601112094 | 0.250073601113749 |


| $\mathbf{x}$ | Analytic solution( $\mathbf{y}_{\mathbf{2}}$ ) | Neural solution <br> (Trainlm) $\left(\mathbf{y}_{\mathbf{2} \mathbf{1}}\right)$ | Neural solution <br> (Trainbfg) <br> $\left(\mathbf{y}_{212}\right)$ |
| :---: | :---: | :---: | :---: |
| 0 | 0 | $1.530880578316805 \mathrm{e}-$ <br> 16 | $-3.059617923823967 \mathrm{e}-12$ |
| 0.1 | 0.128510464762339 | 0.128419804302230 | 0.128510464758401 |
| 0.2 | 0.238619746993297 | 0.238604066374236 | 0.238627462671385 |
| 0.3 | 0.332733745257234 | 0.332733745257234 | 0.332737486328395 |
| 0.4 | 0.412946642430978 | 0.412945914088550 | 0.412946642432535 |
| 0.5 | 0.481081253748791 | 0.481081253748791 | 0.481081253754288 |
| 0.6 | 0.538724152786095 | 0.538724152786095 | 0.538724152783951 |
| 0.7 | 0.587256251241918 | 0.587256251241918 | 0.587254349184960 |
| 0.8 | 0.627879420907607 | 0.627880263180820 | 0.627876612156372 |
| 0.9 | 0.661639670057994 | 0.661639670057993 | 0.661639670057443 |
| 1 | 0.689447320205629 | 0.689447320205629 | 0.689447320203182 |


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| Table (3) : A comparison between analytic and neural solutions |  |  |  |  |  |  |  |  |  |
| $\left\|\mathbf{y}_{2 \mathrm{a}}-\mathrm{y}_{262}\right\|$ |  | $\left\|y_{1 a}-y_{112}\right\|$ |  |  | $\mathbf{y}_{2 a}-y_{2 t 1}$ |  | $\left\|y_{1 a}-y_{1 t 1}\right\|$ |  |  |
| $3.059617923823967 \mathrm{e}-12$ |  | $1.622489973456265 \mathrm{e}-04$ |  |  | 1.530880578316805e-16 |  | 0 |  |  |
| $3.937739023740505 \mathrm{e}-12$ |  | $7.728262474415715 \mathrm{e}-13$ |  |  | 9.066046010927642e-05 |  | $6.899025035600470 \mathrm{e}-05$ |  |  |
| $7.715678088132671 \mathrm{e}-06$ |  | $8.324452238639424 \mathrm{e}-13$ |  |  | $1.568061906176421 \mathrm{e}-05$ |  | 0 |  |  |
| 3.7410711 | 1966758e-06 | $2.143048601244146 \mathrm{e}-06$ |  |  | $5.551115123125783 \mathrm{e}-17$ |  |  |  |  |
| 1.5572543 | 5490476e-12 | $5.532835937183123 \mathrm{e}-07$ |  |  | $7.283424278692330 \mathrm{e}-07$ |  | $7.768340090974490 \mathrm{e}-06$ |  |  |
| 5.4971027 | 2977769e-12 | $2.620459405022757 \mathrm{e}-12$ |  |  | 0 |  | $1.110223024625157 \mathrm{e}-16$ |  |  |
| 2.1445067 | 4365952e-12 | $1.555866546709694 \mathrm{e}-12$ |  |  | 1.110223024625157e-16 |  | 7.437473311000531e-06 |  |  |
| 1.9020569 | 8269505e-06 | $5.691048232669971 \mathrm{e}-08$ |  |  | $2.220446049250313 \mathrm{e}-16$ |  | $5.128752899485889 \mathrm{e}-06$ |  |  |
| 2.8087512 | 25261475e-06 | $4.391098595846188 \mathrm{e}-12$ |  |  | $8.422732126200927 \mathrm{e}-07$ |  | 0 |  |  |
| 5.5055959 | 9116151e-13 | $2.141509192199465 \mathrm{e}-12$ |  |  | 1.110223024625157e-16 |  | 0 |  |  |
| 2.4475976 | 0088620e-12 | $1.654731907052565 \mathrm{e}-12$ |  |  | 1.110223024625157e-16 |  | $5.551115123125783 \mathrm{e}-17$ |  |  |

Table (4): Weight and bias of the network for different training algorithm

| Bias for trainlm of <br> $\left(\mathbf{y}_{\mathbf{1}}\right)$ | Weight for trainlm <br> of $\left(\mathbf{y}_{\mathbf{1}}\right)$ | Weight for trainlm of ( $\mathbf{y}_{\mathbf{1}} \mathbf{)}$ |
| :---: | :---: | :---: |
| Net.B $\{1\}$ | Net. LW\{2,1\} | Net.IW\{1,1\} |
| 0.252859672695871 | 0.017611616453924 | 0.241569248284151 |
| 0.024385651630710 | 0.681708279346507 | 0.351195035228651 |
| 0.530723581584766 | 0.880833084532577 | 0.126738675949935 |
| 0.934854674058909 | 0.139821021807629 | 0.739408639260099 |
| 0.769328503579249 | 0.810853784598876 | 0.445679823858157 |


| bias for trainbfg of $\left(\mathbf{y}_{\mathbf{1}}\right)$ | Weight for trainbfg of $\left(\mathbf{y}_{\mathbf{1}}\right)$ | Weight for trainbfg of $\left(\mathbf{y}_{\mathbf{1}}\right)$ |
| :---: | :---: | :---: |
| Net.B $\{1\}$ | Net. LW\{2,1\} | Net.IW\{1,1\} |
| 0.413824842108441 | 0.67086077132138 | 0.715931222353248 |
| 0.180845024472233 | 0.982859184594668 | 0.248146352936429 |
| 0.995631187232624 | 0.936821328628590 | 0.531900325168972 |
| 0.520386194349656 | 0.576272354062037 | 0.382209682936379 |
| 0.885282695498373 | 0.080186187030087 | 0.801761242973036 |


| Bias for trainbfg of ( $\mathbf{y}_{\mathbf{2}}$ ) | Weight for trainbfg of $\left(\mathbf{y}_{\mathbf{2}}\right)$ | Weight for trainbfg of $\left(\mathbf{y}_{\mathbf{2}}\right)$ |
| :---: | :---: | :---: |
| Net.B $\{1\}$ | Net. LW\{2,1\} | Net.IW\{1,1\} |
| 0.431049305282942 | 0.688725578355128 | 0.869492229395656 |
| 0.190738233247638 | 0.596021891944303 | 0.947906559807061 |
| 0.327775459738820 | 0.214739790766330 | 0.254304842122024 |
| 0.937657078181142 | 0.535169282982425 | 0.048491632422091 |
| 0.847367010662909 | 0.055755557082901 | 0.831838695092381 |


| Weight for trainlm of ( $\mathbf{y}_{\mathbf{2}} \mathbf{)}$ | Weight for trainlm of <br> $\left(\mathbf{y}_{\mathbf{2}}\right)$ | bias for trainlm of ( $\mathbf{y}_{\mathbf{2}} \mathbf{)}$ |
| :---: | :---: | :---: |
| Net.IW\{1,1\} | Net. LW $\{2,1\}$ | Net.B $\{1\}$ |
| 0.101305687973029 | 0.618786526718974 | 0.241305720471971 |
| 0.468935089858187 | 0.699150113317535 | 0.594729968864710 |
| 0.710646362418379 | 0.314828670017582 | 0.868232914442518 |
| 0.601346407503426 | 0.804788645898101 | 0.818668373595483 |
| 0.204916976156494 | 0.178022430412338 | 0.590084132290161 |



Table(5) : The performance of the train with epoch and time

| Train code | Performance for MSE | Time | Epoch | Performance |
| :---: | :---: | :---: | :---: | :---: |
| Trainlm of $\mathrm{y}_{1}$ | $4.010417891598336 \mathrm{e}-10$ | $0: 00: 04$ | 295 | $2.20 \mathrm{e}-33$ |
| Trainlm of $\mathrm{y}_{2}$ | $6.927087884925925 \mathrm{e}-10$ | $0: 00: 06$ | 468 | $3.96 \mathrm{e}-33$ |
| Trainbfg of $\mathrm{y}_{1}$ | $2.154243203877806 \mathrm{e}-09$ | $0: 00: 28$ | 1268 | $5.07 \mathrm{e}-28$ |
| Trainbfg of $\mathrm{y}_{2}$ | $6.957344125042582 \mathrm{e}-12$ | $0: 00: 12$ | 543 | $2.26 \mathrm{e}-25$ |

Table (6) : The analytic \& neural result of the problem (9)

| x | Analytic solution ( $\left.\mathrm{y}_{\mathrm{a} 1}\right)$ | Neural (Trainlm) ( $\left.\mathrm{y}_{1 \mathrm{t} 1}\right)$ <br> solution | Neural (Trainbfg $)\left(\mathrm{y}_{1 \mathrm{t} 2}\right)$ <br> solution |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0.008076966501195 |
| 0.1 | 1.120552473617658 | 1.119074768489855 | 1.121576309950494 |
| 0.2 | 2.096078776007225 | 2.096078776007224 | 2.096078776010794 |
| 0.3 | 2.945348746900685 | 2.945519665978265 | 2.945329004027621 |
| 0.4 | 3.684702961845622 | 3.684702961845623 | 3.684702961851884 |
| 0.5 | 4.328367136833180 | 4.328367136833180 | 4.328367136844937 |
| 0.6 | 4.888725841480949 | 4.888755428434839 | 4.888725841491276 |
| 0.7 | 5.376560787212696 | 5.376560787212696 | 5.376560787208372 |
| 0.8 | 5.801258275273828 | 5.801258275273830 | 5.801258275281827 |
| 0.9 | 6.170989796034165 | 6.171052575520006 | 6.170989796037555 |
| 1 | 6.492869254440744 | 6.492869254440744 | 6.492853256454569 |


| $\mathbf{x}$ | Analytic solution( ya 2$)^{\text {a }}$ | Neural (Trainlm) ( $\mathbf{y}_{21 t}$ ) solution | Neural (Trainbfg) ( $\mathrm{y}_{2 \mathrm{t} 2}$ ) solution |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | $6.970449786967482 \mathrm{e}-08$ |
| 0.1 | 0.079077570606103 | 0.083579667139451 | 0.079077614840971 |
| 0.2 | 0.301069405674204 | 0.301069405674204 | 0.296617057945247 |
| 0.3 | 0.645370996519114 | 0.645370996519114 | 0.643383165800754 |
| 0.4 | 1.094073563826115 | 1.094073563826114 | 1.094073602030272 |
| 0.5 | 1.631614766704876 | 1.629619175798611 | 1.631757503744028 |
| 0.6 | 2.244474623805575 | 2.242721178439358 | 2.244474633309778 |
| 0.7 | 2.920910794904590 | 2.920910794904590 | 2.920910793699243 |
| 0.8 | 3.650728128703034 | 3.650322736313918 | 3.650728106463634 |
| 0.9 | 4.425078041900662 | 4.425078041900662 | 4.425158477200711 |
| 1 | 5.236283868595361 | 5.236283868595361 | 5.236283818105677 |

Table (7) : A comparison between analytic and neural solutions

| $\left\|y_{2 a}-y_{2 t 2}\right\|$ | $y_{1 a}-y_{162} \mid$ | $y_{2 a}-y_{2 t 1} \mid$ | $\left\|y_{1 a}-y_{1 t 1}\right\|$ |
| :---: | :---: | :---: | :---: |
| 6.970449786967482e-08 | 0.008076966501195 | 0 | 0 |
| 4.423486724136616e-08 | 0.001023836332836 | 0.004502096533347 | 0.001477705127803 |
| 0.004452347728957 | 3.569144979564953e-12 | 6.106226635438361e-16 | $4.440892098500626 \mathrm{e}-16$ |
| 0.001987830718360 | 1.974287306349964e-05 | 0 | 1.709190775800451e-04 |
| 3.820415694910651e-08 | 6.261213769676033e-12 | 6.661338147750939e-16 | $4.440892098500626 \mathrm{e}-16$ |
| $1.427370391517968 \mathrm{e}-04$ | 1.175681774157056e-11 | 0.001995590906265 | 0 |
| 9.504203646315545e-09 | 1.032685048585336e-11 | 0.001753445366216 | $2.958695388954880 \mathrm{e}-05$ |
| 1.205346933375040e-09 | $4.324540725519910 \mathrm{e}-12$ | 0 | 8.881784197001252e-16 |
| $2.223940009926650 \mathrm{e}-08$ | 7.998046669399628e-12 | $4.053923891160771 \mathrm{e}-04$ | 1.776356839400251e-15 |
| 8.043530004897548e-05 | 3.389288849575678e-12 | 0 | 6.277948584099136e-05 |
| $5.048968443333024 \mathrm{e}-08$ | 1.599798617490933e-05 | 0 | 0 |



Table( 8): Weight and bias of the network for different training algorithm

| Bias for trainlm of <br> $\left(\mathbf{y}_{\mathbf{1}}\right)$ | Weight for trainlm of <br> $\left(\mathbf{y}_{\mathbf{1}}\right)$ | Weight for trainlm of <br> $\left(\mathbf{y}_{\mathbf{1}}\right)$ |
| :---: | :---: | :---: |
| Net.B $\{1\}$ | Net. LW\{2,1\} | Net.IW\{1,1\} |
| 0.134776995255468 | 0.792456860497627 | 0.505692448683919 |
| 0.569914349014358 | 0.837900449095441 | 0.004625760582352 |
| 0.574691506274377 | 0.687358399403697 | 0.188468748383506 |
| 0.016102750791896 | 0.081434100056796 | 0.779639443833603 |
| 0.934828315776462 | 0.806140569013718 | 0.610825949687488 |


| Weight for trainlm of <br> $\left(\mathbf{y}_{\mathbf{2}}\right)$ | Weight for trainlm of <br> $\mathbf{( \mathbf { y } _ { \mathbf { 2 } } )}$ | bias for trainlm of <br> $\left(\mathbf{y}_{\mathbf{2}}\right)$ |
| :---: | :---: | :---: |
| Net.IW $\{1,1\}$ | Net. LW $\{2,1\}$ | Net.B $\{1\{$ |
| 0.478376283649921 | 0.922429224841606 | 0.912782147048597 |
| 0.124994240255344 | 0.934308461414860 | 0.534170292387813 |
| 0.064155985584096 | 0.824811938202454 | 0.451461598784967 |
| 0.386664880532908 | 0.183582125058882 | 0.285596533472468 |
| 0.558245691279696 | 0.393108093448545 | 0.622774097441083 |


| Bias for trainbfg of ( $\mathbf{y}_{\mathbf{2}}$ ) | Weight for trainbfg of $\left(\mathbf{y}_{\mathbf{2}}\right)$ | Weight for trainbfg of $\mathbf{( y}_{\mathbf{2}} \mathbf{)}$ |
| :---: | :---: | :---: |
| Net.B\{1\} | Net. LW\{2,1\} | Net.IW\{1,1\} |
| 0.612551084945355 | 0.002291815245818 | 0.018010467945131 |
| 0.133072433875949 | 0.772712775811915 | 0.503631782070622 |
| 0.283353859003173 | 0.661798871106240 | 0.126991991291519 |
| 0.837400333016416 | 0.397966331038198 | 0.305174566418702 |
| 0.865931228918039 | 0.501051178487892 | 0.256058502513567 |


| Bias for trainbfg of ( $\mathbf{y}_{\mathbf{1}}$ ) | Weight for trainbfg of $\left(\mathbf{y}_{\mathbf{1}}\right)$ | Weight for trainbfg of $\left(\mathbf{y}_{\mathbf{1}}\right)$ |
| :---: | :---: | :---: |
| Net.B\{1\} | Net. LW\{2,1\} | Net.IW $\{1,1\}$ |
| 0.828924078623420 | 0.100480242633400 | 0.735194614493405 |
| 0.724963349991644 | 0.522668514129408 | 0.879697065220770 |
| 0.337293776914633 | 0.058688252904172 | 0.851423388162803 |
| 0.211463983876867 | 0.813646068464573 | 0.672029350928386 |
| 0.339840122932540 | 0.345685331495202 | 0.798496214678467 |

Table (9) : The performance of the train with epoch and time

| Performance for MSE | Time | Epoch | Performance | Train code |
| :---: | :---: | :---: | :---: | :---: |
| $1.814434713408252 \mathrm{e}-07$ | $0: 00: 05$ | 302 | $2.82 \mathrm{e}-32$ | Trainlm of y1 |
| $2.249195719271235 \mathrm{e}-06$ | $0: 00: 02$ | 102 | $4.83 \mathrm{e}-32$ | Trainlm of y2 |
| $5.423422452091749 \mathrm{e}-06$ | $0: 00: 35$ | 1461 | $2.49 \mathrm{e}-26$ | Trainbfg of y1 |
| $1.947413043462885 \mathrm{e}-06$ | $0: 00: 05$ | 243 | $2.20 \mathrm{e}-23$ | Trainbfg of y2 |


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Fig. (1): decongestant in GI tract(solid)and bloodstream(dashed):single unit dose ( $k_{1}=1.386, k_{2}=0.1386$ )


Fig. (2): Decongestant in GI tract (solid) and bloodstream (dashed) : continuous acting capsules ( $\mathrm{k}_{1}=1.386, \mathrm{k}_{2}=0.1386$ ) , $\mathrm{I}=12$.





Fig. (3): Decongestant in GI tract (solid) and bloodstream (dashed): continuous acting capsules ( $\mathrm{k}_{1}=1.386, \mathrm{k}_{2}=\mathbf{0 . 1 3 8 6}$ ) , $\mathrm{I}=6$

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| No. | 3 | Vol. | 25 | Year | 2012 | 2012 | السنة | 25 | المجلد | 3 | (العدد |

## تصميم شبكة عصبية صناعية ذو تغذية تقدمية لتحديد جرعات دواء الايكونجيستد

لمى ناجي محمد توفيق و يسر رافد بحر المعيوف قسم الرياضيات، كلية التربيةـ ابن اللهيثّ، جامعة بغداد استلم البحث في:30 ايار 2012 قبل البحث في : 24 ايلول 2012

الخلاصة

الهدف من هذا البحث هو تصميم شبكة عصبية صناعية ذو تغذية تقىمية لتحديد نأثير حبوب البرد و تعاقبها من خلال استخدام النمذجة و تحويل المشكلة إلى منظومة معادلات مسائل القيم الابتدائية من الرتبة الأولى ـ هذه المسألة مثال لعدد من النماذج التي تمثل مرور العلاج خلال الجاسم. الانموذج الصصمم هو جزء مهم في العلاج والذي يحدد مستوى الجرعات و معدلها حيثٌ ان التحليل الحرج هو الحاجة لبقاء مسنوى العلاج عال و فعال لكن ليس العلو الذي يجعله خطر الكلمات المفتاحية:. الشبكة العصبية، الثبكة العصبية التققمية،استخدام النمذجة .

