



Fatigue life prediction of 5083 and 5A06 aluminum alloy T-welded joints based on the fatigue characteristics domain

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ABSTRACT. Three-point bending fatigue test of 5083 and 5A06 aluminum alloy T-welded joints is carried out, and the fatigue life of the specimens with different influencing factors are obtained. Finite element model of the T-welded joint is established and the nodal force based structural stress is calculated. Neighborhood rough set theory is used for analysis of the factors which influence the fatigue life of the aluminum alloy welded joints. Key influencing factors are studied and the fatigue characteristic domains are determined. The master S-N curve characterized by the nodal force based structural stress range and cycles to failure on bi-logarithmic coordinate as well as S-N curves corresponding to the fatigue characteristic domain are fitted. A case study of fatigue life prediction of 5A06 aluminum alloy welded joint indicates the effectiveness of the fatigue life prediction method based on the fatigue characteristic domain.



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KEYWORDS. Fatigue life; Welded joints; Fatigue characteristic domain.

INTRODUCTION

aster S-N curve method, also called equivalent structural stress method or nodal force based structural stress method is a new type of fatigue life prediction technology for welded structures proposed by Dong etc. [1, 2] at the beginning of this century. The structural stress calculated in the master S-N curve method is mesh-



insensitive, so it is intrinsic to a given joint geometry and loading mode [3]. Due to the mesh-insensitive structural stress calculation, its high precision and widely applicability, the master S-N curve method is one of the most attractive fatigue analysis engineering technologies for welded structures in the world. For example, master S-N curve in ASME code is used for life evaluation for plane steel gate [4]. Hong and Cox [5] proposed a procedure for fatigue behavior of welded joints with multi-axial stress states by using an effective equivalent structural stress range parameter combined normal and in-plane shear equivalent structural stress ranges. They suggested that it could be generally applicable to predict the failure location and the fatigue life at welds of interest. The application of the master S-N curve approach for fatigue analysis of breathing webs through FE simulation of multiple plate girders is illustrated and the effect of initial out-of-plane displacement as an important geometrical parameter in the girders' fatigue behavior is investigated by Mojgan [6]. A simplified version of master S-N curve method, which needs even less experimental input, using an assumption of constant S-N curve slope is presented by Atul [7]. Dong etc. have carried on the reprocessing of thousands of fatigue test results data of steel structure welded joint in the last 50 years. The master S-N curve for fatigue design based on equivalent structural stress range is determined by linear regression analysis. Statistical results show that the scatter level of all S-N samples represented by standard deviations is about 0.25 [8]. In order to further reduce the scatter degree of S-N curves and to improve the fatigue life prediction accuracy, rough set theory is used for analysis of the factors which influence the fatigue life of the aluminum alloy welded joints.

Rough set theory (RST) [9], proposed by Pawlak, has been successfully used as a new feature reduction tool to discover data dependencies and reduce the number of features contained in a dataset. The traditional RST-based feature reduction algorithms are established on the equivalence relation and only compatible for categorical datasets. Discretization should be conduct when processing continuous numerical data, which would lead to losing of information [10, 11]. To overcome this drawback, many extensions of RST have been proposed, such as fuzzy rough sets [12, 13], tolerance approximate models [14, 15], covering approximate model [16, 17] and neighborhood granular model [18, 19]. Among all the extensions, neighborhood rough set model can process both numerical and categorical data set via the δ -neighborhood set, which will not break the neighborhood and order structure of dataset in real spaces [20]. To reduce information loss, neighborhood rough set theory is used here to determine the fatigue characteristics domain.

Three-point bending fatigue test of 5083 and 5A06 aluminum alloy T-welded joints is carried out in this work to further demonstrate the applicability and validity of the S-N curve modeling method based on the fatigue characteristics domain. Fatigue characteristic domains are determined and a set of S-N curves correspond to the different fatigue characteristic domain are obtained. Statistical analysis is carried out and a case study of fatigue life prediction of 5083 aluminum alloy T-welded joint is conducted. The results of case study show that the predicted result is in good agreement with the test result.

METHODOLOGY

Basic Principle of the master S-N curve approach

he nodal force based structural stress method is based on equilibrium-equivalent decomposition of an arbitrary stress state at a location of interest such as at weld toe (Fig. 1) into an equilibrium-equivalent structural stress part and a self-equilibrating notch-stress part [3]. The equivalent structural stress is described as

$$\sigma_s = \sigma_m + \sigma_b$$



Figure 1: Stress distribution at the weld toe.

(1)



Suppose *l* represents the length of the weld toe line, the plate thickness is *t*, the force vertical to the welding toe is F_j , the bending moment around the welding toe is M_x , f_j is line force and m_x is line moment, according to the mechanical formula of the material as shown in Eqn. (2), the structural stress can be calculated as Eqn. (3) and (4).

$$\sigma_m = \frac{Fy}{A} = \frac{Fy}{l \cdot t} \quad , \sigma_b = \frac{M_x}{W} = \frac{M_x}{\frac{1}{6} \cdot l \cdot t^2}$$
(2)

$$f_{y} = F_{y} / l \quad , \quad m_{\chi} = M_{\chi} / l \tag{3}$$

$$\sigma_s = \sigma_m + \sigma_b = \frac{f_y}{t} + \frac{6m_x}{t^2} \tag{4}$$

An equivalent structural stress range parameter can be defined as:

$$\Delta S_{s} = \frac{\Delta \sigma_{s}}{\frac{2-m}{t \ 2m} \cdot I(r)m}$$
(5)

where $\Delta \sigma_s$ represents the structural stress range calculated, I(r) is a dimensionless parameter derived by fracture mechanics considerations, and *m* is the crack propagation exponent in the conventional Paris law, taking on a value of about 3.6 [21]. It could be seen that the equivalent structural stress parameter described in Eqn. (5) can capture the effects of stress concentration, plate thickness and loading mode effects on fatigue behavior of welded components.

The formula for fatigue life calculation of welded joints using the equivalent structural stress ΔS_c can be expressed as

$$\Delta S_{s} = C N^{h} \tag{6}$$

where N is the number of cycles which indicate the fatigue life of the structure, C is material constant and h represents the negative slope of the master S-N curve. By performing regression analysis with respect to the cycles to failure, Tab. 1. summarizes the statistical parameters of the master S-N curve in terms of the mean, $\pm 1\sigma$, $\pm 2\sigma$, $\pm 3\sigma$ [21].

Statistical Basis	Ferritic and stainle	ess Steels	Aluminum	
	С	h	С	h
Mean	19930.2		3495.13	
+1σ (upper 68%)	23885.8		4293.19	
-1σ (lower 68%)	16629.7		2845.42	
+2σ (upper 95%)	28626.5	-0.32	5273.48	-0.28
-2σ (lower 95%)	13875.7		2316.48	
+3σ (upper 99%)	34308.1		6477.60	
-3σ (lower 99%)	11577.9		1885.87	

Table1: Coefficients of master S-N curve.

Fatigue characteristics domain

Rough set theory can objectively obtain the key fatigue life influencing factors set of welded joints from the data of fatigue test specimens of welded joints. The fatigue samples with the same value of the key fatigue life influencing factors of the welded joints are distributed in a relatively independent area, which is called fatigue characteristics domain. The calculation



of weights is a quantitative description of the extent to which various key influencing factors affect fatigue life. If there are too many key fatigue life influencing factors in the neighborhood rough set attributes reduction results, the number of the key factors could be appropriately reduced by increasing the criticality threshold of the influencing factors so as to reduce the number of the fatigue characteristics domains. The basic process for determine of the fatigue characteristics domains is shown in Fig. 2.



Figure 2: Process of determining of the fatigue characteristics domain.

Among all the steps in the process of determining the fatigue characteristics domain, the neighborhood attributes reduction step is the most important. A forward greedy algorithm is used for attributes reduction as described in [21]. The forward greedy algorithm includes the following 7 steps.

Step 1: Input the fatigue decision system $\langle U, C, D, \delta \rangle$ and the attribute importance threshold ε . Where $U = \{x_1, x_2, ..., x_n\}$ is a nonempty finite set of objects called the universe, C is the condition features set, $C = \{a_1, a_2, ..., a_n\}$, D is the set of decision features, and δ is the neighborhood parameter $(0 \le \delta \le 1)$. For the fatigue decision system here, U is the set of all the fatigue specimens, C is the set of the fatigue life influencing factors of the welded joints, D is the fatigue life of the welded joints.

Step 2: For each condition attribute $a_i \in C$, compute the neighborhood radius $\delta(a_i) = STD(a_i) / \lambda$, where $STD(a_i)$ represents the average value of the attribute a_i , and λ is a neighborhood radius calculation parameter, its value is usually between 2~4.

Step 3: Let $\phi \rightarrow RED$.

Step 4: For each $a_i \in C - \operatorname{Re} d$ compute the significance of a_i , $SIG(a_i, \operatorname{Re} d, D) = \gamma_{\operatorname{Re} d \cup a_i}(D) - \gamma_{\operatorname{Re} d}(D)$ where

 $\gamma_{\text{Re}d}(D) = \frac{|\underline{N} \operatorname{Re}dD|}{|U|} \text{ is attribute dependence, } \underline{N}_{\text{Re}d}D = \{x_i \mid \delta_{\text{Re}d}(x_i) \subseteq D, x_i \in U\} \text{ is the lower approximate set,}$

 $\delta(x_i) = \{x \in U, \Delta(x, x_i) \le \delta\}, \Delta(x, y)$ is a distance function, which satisfies

- (1) $\Delta(x, y) \ge 0$;
- (2) $\Delta(x, y) = 0$, if and only if x=y;
- (3) $\Delta(x, y) = \Delta(y, x);$
- (4) $\Delta(x, y) + \Delta(y, z) \ge \Delta(x, z)$.

Step 5: Select the attribute a_k with the maximum significance value in the conditional attribute sets.

Step 6: Determine whether the significance value of the attribute a_k is greater than the given threshold value, if it is true then go to step 4, otherwise go to step 7.

Step 7: Return the reduction results RED, exit.



EXPERIMENT

These-point bending fatigue experiment is carried out to test the fatigue life of specimens. First of all, material of the specimens and welding technology are introduced, then the three-point bending fatigue test of aluminum alloy T-welded joints is described, after that finite element model of T-joint is established, hot spot stress is calculated and equivalent structural stress transformation is accomplished. Master S-N curve for design together with the S-N curves cluster according to the fatigue characteristic domain are fitted. Finally, the S-N curve cluster and the master S-N curve are compared and a case study is analyzed.

Material of the specimens

Materials of the specimens used in the experiment are 5083 and 5A06 aluminum alloy. These two kinds of aluminum alloy belong to non-heat treatment aluminum alloy material in Al-Mg alloy. The chemical composition and mechanical properties of the materials are shown in Tab. 2 and Tab. 3 respectively.

The welding material is 5183 aluminum alloy welding wire and the diameter of the welding wire is 1.2 mm. The chemical composition of deposited metal is shown in Tab. 4, and the protective gas used is Ar.

Mater	rial Brand	Si	Fe	Cu	Mn	Mg	Cr	Zn	Ti	Al
5083	measured	0.1	0.25	0.04	0.62	4.68	0.11	0.02	0.10	other
5005	standard	≤0.40	≤0.40	≤0.10	0.40~1.0	4.0~4.9	$0.05 \sim 0.25$	≤0.25	≤0.15	other
5 4 0 6	measured	0.15	0.25	0.05	0.62	6.54	/	0.02	0.04	other
3A00	standard	≤0.40	≤0.40	≤0.10	$0.50 \sim 0.80$	5.8~6.8	/	≤0.20	0.02~0.10	other

Table 2: Chemical composition of test materials (%).

		Tensile test						
Material Brand	Thickness / <i>mm</i>	R _m /MPa	R _{p0.2} /MPa	A /%	Bend diameter /mm	Bend angle /°	result	Hardness HB
	6	350	220	17.5	36	180	No cracks	84.4
5083		345	220	15.5			No cracks	
0000	10	320	192	19.5	60	180	No cracks	79.1
		320	195	19.0			No cracks	
	6	345	177	24.5	36	180	No cracks	84.9
	0	345	184	18.5	50	100	No cracks	04.7
F A O C	12	350	166	26.0	72	180	No cracks	83.0
5A06	12	350	168	27.0	12	100	No cracks	03.9
	16	345	154	28.0	96	180	No cracks	83.9
		345	154	29.5			No cracks	

Table 3: Mechanical properties of test materials.

Material name	Si	Cu	Mn	Mg	Cr	Zn	Al
5183	0.4	0.10	0.5~1.0	4.3~5.2	0.05~0.25	0.25	other

Table 4: Chemical composition of 5183 aluminum alloy welding wire.



Welding process

MIG welding method with the Austria Fronius welding machine is used in the experiment here. The T-welded joints specimen has K type groove, the groove angle is 55°, without leaving blunt edge, the interval is 1-2mm, tests of the T-joints made of 5083 and 5A06 aluminum alloy with different thickness are carried out respectively. X - ray flaw detection is carried out after welding, and three-point bending fatigue experiment of 5A06+5083 T-joint and 5A06+5A06 T-joint are made. The relevant welding parameters of the T-joints are shown in Tab.5.

Material	Thickness /mm	Groove form	Layers	Welding current /A	Welding voltage /V	Welding speed /mm/s	Gas flow /L/min	X ray flaw detection rating
			1	210	24.2	7.0	20	
5A06+	16+10	V	2	240	24.8	7.45	20	т
5083	10+10	K	3	220	26.6	4.61	20	11
			4	220	26.6	4.56	20	
			1	220	26.6	7.29	20	
			2	236	24.8	7.78	20	
5A06+	25 + 17	V	3	220	26.6	5.93	20	т
5A06	35+16	6 K	4	220	26.6	5.30	20	1
			5	220	27.4	5.30	20	
			6	220	27.4	4.86	20	

Table 5: Welding parameters of T-welded joints.

Three-point bending fatigue test of T-joint

The experiment is carried out in accordance with JB/T7716-95. Size and shape of the specimen in the three-point bending fatigue test are shown in Fig. 3. The thickness of the T-welded joint expressed as *a* in Fig. 3. In this work, the nominal value of *a* is 8.6mm for the 5A06+5083 T-joint and it is 14.9mm for the 5A06+5A06 T-joint. PLG-100 microcomputer controlled high frequency fatigue testing machine is used for the three-point bending fatigue test of T-joint. Other technical specifications in the test are: the precision of the static load is $\pm 1\%$, the average fluctuation of dynamic load is $\pm 1\%$, the amplitude fluctuation of dynamic load is $\pm 2\%$. The loading mode of the three-point bending fatigue test is shown in Fig. 4. Span of fulcrum of the 5A06+5A06 T-joint is 100mm, and that of the 5A06+5083 T-joint is 60 mm. Vibration frequency for 5A06+5A06 T-joint is 170HZ, and for 5A06+5083 T-joint, it is 160HZ. During the test, when the crack size at the weld toe is large enough causing the load not to go up, automatically unload and stop vibration, then record the cycle times. The cyclic stress ratio used in the test is R=0.1, and the designated cycle life is 1×10^7 .

Ten 5A06+5A06 and ten 5A06+5083 T-joints specimens are used in the three-point bending fatigue test. Fatigue life data of the specimens obtained in the test are shown in Tab. 6.



Figure 3: Size and shape of the three-point bending fatigue specimen.



Figure 4: Loading mode of T-joint specimen.

Material	Specimen number	Load frequency (<i>HZ</i>)	σ _{max} MPa	Cycle numbers when crack (×10 ⁶)	Fracture location	note
	1-1	163	75.0	0.4521	weld toe	
	1-2	174	70.0	0.9885	weld toe	Clip holding problem
	1-3	171	80.0	0.2257	weld toe	
	1-4	151	60.0	> 10	without fracture	
	1-5	150	70.0	2.08	weld toe	
5A06+5083	1-6	159	60.0	3.3749	weld toe	
	1-7	163	55.0	> 10	without fracture	
	1-8	162	60.0	4.3542	weld toe	
	1-9	159	55.0	> 10	without fracture	
	1-10	171	60.1	5.7485	weld toe	
	2-1	158	80.0	0.2729	weld toe	
	2-2	158	70.0	0.7759	weld toe	
	2-3	159	40.0	8.7281	weld toe	
	2-4	164	35	> 10	without fracture	
	2-5	170	37.5	> 10	without fracture	Weld toe is not fused
5A06+5A06	2-6	172	40.0	4.3287	weld toe	
	2-7	172	37.5	9.3184	weld toe	There is a scratch 2 mm around the weld toe
	2-8	170	35	> 10	without fracture	
	2-9	170	37.5	> 10	without fracture	
	2-10	170	40.0	6.3685	weld toe	

Table 6: Three-point bending fatigue test data of T-joints.

where σ_{max} is computed through Eqn. (7)~(9), which is the maximum bending fatigue stress, *M* is the maximum bending moment, ω is the anti-bending section coefficient, *F* is the load applied, *L*_S is the distance between pivots, *b* is the width of the specimen, *b* is the thickness of the specimen.

$$\sigma_{\max} = \frac{M}{\omega} \tag{7}$$

$$M = \frac{FL_S}{4} \tag{8}$$



(9)

$$\omega = \frac{bb^2}{6}$$

Finite element model of T-joints

Material properties used in the FE analysis are shown in Tab.7 and the finite element type is C3D8R. The size of the mesh refinement will not influence the calculation result of the nodal force based structural stress and the element size is not unified here. According to the size of the specimens of 5A06+5083 T-joint and 5A06+5A06 T-joint, the corresponding finite element model is established as shown in Fig. 5 and Fig. 6. Position of the fulcrum in the test is determined according to JBT 7716-1995. For the 5A06+5083 T-joints, the span of fulcrum is 60 mm, and for the 5A06+5A06 T-joints, the span of fulcrum is 100mm. The loading mode of the 5A06+5083 T-joint is shown in Fig. 7.

Material	Density (Kg/mm³)	Young modulus (MPa)	Poisson ratio
5A06	2.7e-9	71000	0.33
5083	2.72e-9	71016	0.33
5183	2.66e-9	70327	0.33









Figure 6: Finite element model of 5A06+5A06 T-joint.



Figure 7: Loading position of 5A06+5083 T-joint.

Structural stress computation

ABAQUS software is used to simulate the 5A06+5083 T-joint and the 5A06+5A06 T-joint so that the nodal force at weld toe is computed. The detailed calculation process of structural stress and equivalent structural stress could be found in reference [1,2]. For example, the nodal force computation result of 5A06+5083 T-joint when $\sigma_{max} = 70MPa$ and the nodal force computation result of 5A06+5083 T-joint when $\sigma_{max} = 80MPa$ are shown as in Fig. 8 and Fig. 9. The thickness of the 5A06+5083 T-joint shown as *a* in Fig. 3 is 8.6 mm and it is 14.9 mm for the 5A06+5A06 T-joint.







Figure 8: Stress results of 5A06+5083 T-joint.

Figure 9: Stress results of 5A06+5A06 T-joint.

According to the results of nodal force, Verity module in the FE-SAFE software is used for structural stress computation and equivalent structural stress transformation at weld toe. Computation results of the 5A06+5083 T-joint and 5A06+5A06 T-joint are obtained as shown in Tab.8.

Material	Specimen number	σ _{max} MPa	Structural stress (MPa)	Equivalent structural stress range (MPa)	Cycle numbers when crack (×10 ⁶)
	1-1	75	51.99	81.19	0.4521
5A06+5083	1-3	80	55.45	86.61	0.2257
	1-5	70	48.52	75.78	2.08
	1-7	60	41.59	64.95	4.3542
	1-9	60	41.59	64.95	3.7642
	1-11	60.1	42.28	66.04	5.7485
	2-1	80	74.75	129.69	0.2729
	2-2	60	56.06	97.27	1.3366
5A06+5A06	2-3	50	46.72	81.06	2.3358
	2-4	40	37.38	64.85	8.7281
	2-7	40	37.38	64.85	4.3287
	2-11	40	37.38	64.85	6.3685

Table 8: Computation results of structural stress and equivalent structural stress range.

RESULTS

Master S-N curve for fatigue design

A coording to the results of three-point bending fatigue test and the data collected from related literatures [22-25], fatigue database of aluminum alloy welded joints is established. Some of the data in the database are shown in the following Tab.9. There are 76 samples in the database including 7 types of materials, 4 kinds of welding methods, 6 types of plate thickness whose range is from 2.5mm to 16mm, three cases of stress ratio including 0, 0.1 and 0.5, 3 kinds of loading type including tensile(T), four point bending (4B) and three-point bending(3B), 3 kinds of joint type including T-joints, lap joints and butt joints.

The fatigue test data of aluminum alloy welded joints is analyzed by using MATLAB software, and S-N curve is expressed in the form of $\lg S = A + B \lg N$. On bi-logarithmic coordinate, mean S-N curve of the test samples based on



equivalent structural stress range is fitted by using least square method as Mean1 in Fig. 10. Mean of the master S-N curve defined in Tab. 1 is shown as Mean2 in Fig. 10. Goodness-of-fit statistics of Master S-N curve by using Eq.SS Range is shown in Tab.10. For more detailed about the definition of *SSE*, *R-square*, *Adjusted R-square* and *RMSE*, please see reference [26].



Figure 10: Master S-N curve based on Eq. SS Range.

Material	Welding	Thickness	Ratio	Loading	Joint	Equivalent structural stress	Life
type	method	(mm)		type	type	range(MPa)	cycles
5083 H11	MIG	10	0.1	4B	TJ:p	187.6994	29250
5083 H11	MIG	10	0.1	4B	TJ:p	160.8852	55000
AlMg4MnCr	GMAW	2.5	0.1	Т	LJ_SS:p	154.7135	20540
AlMg4MnCr	GMAW	2.5	0.1	Т	LJ_SS:p	85.0924	121730
AlMgSi1 (6082)	TIG	3	0	Т	LJ_DS:p	294.1392	13250
AlMgSi1 (6082)	TIG	3	0	Т	LJ_DS:p	159.7613	85920
NP5/6	Manual Arc	4.76	0	Т	SJ_DS:p	154.9481	90000
HP30	Manual Arc	4.76	0	Т	SJ_DS:p	116.2111	188000
5A06+5083	MIG	10	0.1	3B	Т	81.19	452100
5A06+5A06	MIG	16	0.1	3B	Т	129.69	272900

Table 9: Fatigue data of aluminum alloy welded joints.

	Mean value
SSE	0.4389
R-square	0.7929
Adjusted R-square	0.7901
RMSE	0.0770

Table 10: Goodness-of-fit statistics of master S-N curve by using Eq.SS range.

Expression of the mean S-N curve of aluminum alloy welded joint based on the Eq.SS range obtained in the experiment is shown as the following Eqn.(10).



$\lg \Delta S = 3.144 - 0.2018 \lg N$

(10)

S-N curves cluster based on fatigue characteristic domain

Neighborhood fatigue decision system is constructed according to the established fatigue database of aluminum alloy welded joints. Feature reduction of this neighborhood fatigue decision system is accomplished by using the forward greedy algorithm. The reduction result we get in the experiment is {Material type, Ratio, Equivalent structural stress range}. Accordingly, fatigue characteristic domain is divided based on the reduction result and we get the 8 fatigue characteristic domains from S_1 to S_8 . In domain S_1 , material type is 5083H11 and ratio is 0.1. In domain S_2 , material type is 5083H11 and ratio is 0.5. In domain S_3 , material type is AlMg4MnCr and ratio is 0.1. In domain S_4 , material type is AlMg51(6082) and ratio is 0. In domain S_5 , material type is NP5/6 and ratio is 0. In domain S_6 , material type is 5A06+5083 and ratio is 0.1. In domain S_6 , material type is 0.1. S-N curves are fitted in each fatigue characteristic domain, and the S-N curves cluster we get in the experiment are shown in Fig. 11. Where Mean₇ and Mean₈ corresponds to the 5A06+5083 and the 5A06+5A06 T-joints respectively. Goodness-of-fit statistics of Mean₇ and Mean₈ are shown in Tab. 11.



Figure 11: S-N curve cluster based on the fatigue characteristic domain.

	Mean ₇	Mean ₈
SSE	0.0012	0.0029
R-square	0.9202	0.9555
Adjusted R-square	0.9002	0.9406
RMSE	0.0173	0.0311

Table 11: Goodness-of-fit statistics of Mean7-Mean8.

The S-N curve equation of Mean₇ and Mean₈ are shown as the following (11) and (12).

$$\lg \Delta S = 2.426 - 0.0907 \lg N \tag{11}$$

$$\lg \Delta S = 3.302 - 0.2183 \lg N \tag{12}$$

From the process of the determination of the fatigue characteristic domains we could see that neighborhood rough set reduction result is the foundation of determination of fatigue characteristic domains. By using neighborhood rough set theory, we don't depend on any prior knowledge to achieve the classification of the welded joint fatigue samples. Each



class of welded joint fatigue test samples forms a relatively independent sample space, which is called fatigue characteristic domain. S-N curve cluster could be obtained by fitting the S-N curve in each fatigue characteristic domain. The fatigue life of welded joints is evaluated based on the fitted S-N curve cluster, which can further reduce the dispersion degree of fatigue test samples and improve the prediction accuracy of fatigue life of welded joints.

It could be seen from Fig. 11, under semi-log coordination, fatigue test samples of aluminum alloy welded joints with different types of materials, under different stress ratio distributed in a relatively independent space, which is called the fatigue characteristic domain. S-N curve cluster is obtained by fitting the S-N curve in each fatigue characteristic domain, Mean₁~Mean₈. From Tab.10 and Tab. 11, we could find that *SSE* and *RMSE* of Mean₇ and Mean₈ are both smaller than that of the Mean, while *R-square* and *Adjusted R-square* of Mean₇ and Mean₈ are both closer to 1 than that of the Mean. Smaller *SSE* and *RMSE*, bigger *R-square* and *Adjusted R-square*s indicate that S-N curves fitted based on the characteristic domain have better performance and higher prediction accuracy.

Case study

To further verify the effectiveness of the fatigue life prediction method based on the fatigue characteristics domain, under the same experiment conditions, take one 5A06+5A06 T-joint specimen as example. The three-point bending fatigue test of the welded joint is carried out. Fatigue life prediction of the T-joint by using master S-N curve is compared with the prediction value by using S-N curve Mean₈ based on the fatigue characteristic domain and the actual value obtained in the fatigue test. The number of cycles to failure of the specimen is 249363 according to Eqn. (10) and it is 516050 by using Eqn. (12). Comparison result show that fatigue life prediction value of the T-joint by using S-N curve Mean₈ is in better agreement with the experiment results than by using the master S-N curve. Actual fatigue life of the test case is shown in Tab. 12.

Material type	Welding method	Thickness (<i>mm</i>)	Ratio	Loading type	Joint type	Equivalent structural stress range (MPa)	Life cycles
5A06+5A06	MIG	16	0.1	3B	Т	113.48	775900

Table 12: Fatigue test data of aluminum alloy T-welded joints.

DISCUSSION AND CONCLUSION

The hree-point bending fatigue test of aluminum alloy T-welded joint of 5083 and 5A06 is carried out. The finite element model of T-joints is established, and the equivalent structural stress is calculated. The master S-N curve for fatigue design and the S-N curves cluster in different fatigue characteristic domains are fitted according to the experimental fatigue data and the data collected from the literatures. Goodness-of-fit statistics results indicate that the S-N curve cluster has higher prediction accuracy than the master S-N curve. The case study of fatigue life prediction of 5A06+5A06 aluminum alloy T-welded joint specimen show fatigue life prediction by using the S-N curves cluster is in better agreement with the experimental results.

Neighborhood rough set theory could find the core factors which influence the fatigue life of the aluminum alloy Twelded joints from the data itself without any prior experience. Fatigue characteristics domain of aluminum alloy Twelded joints could be determined based on reduction results of the neighborhood rough set theory. The result of the case study show that the dispersion level of fatigue samples is further reduced and the fatigue life prediction accuracy is further improved.

Future work will be concentrated on the further validation of the fatigue life prediction method based on the fatigue characteristics domain in the practical engineering.

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